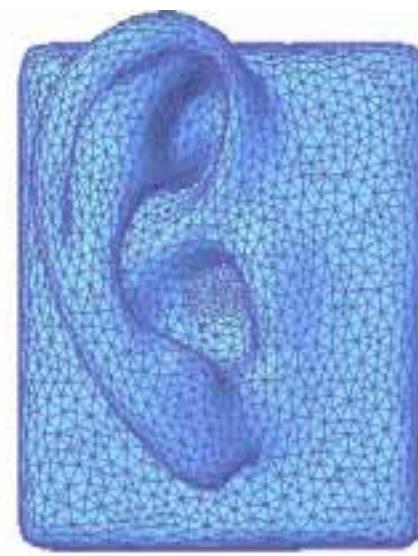
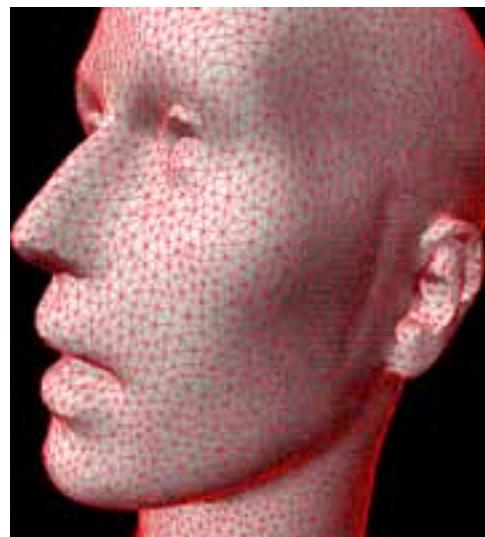


Numerical Modelling of the Head-Related Transfer Function

Yuvi Kahana

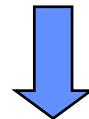


First Question

Can we obtain individualised HRTFs
without a single acoustic measurement ?

Method

Convert the **geometry** of an object
(head+pinna) into its **acoustic** response



Solve the wave equation

PREVIOUS WORK

Weinrich (1984)

“The rather complicated shape of the pinna makes a rigorous mathematical treatment very difficult - perhaps impossible”

Shin-Cunningham and
Kulkarni (1996)

“Theoretically, it is possible to specify the pressure at the eardrum for a source from any location simply by solving the wave equation...”

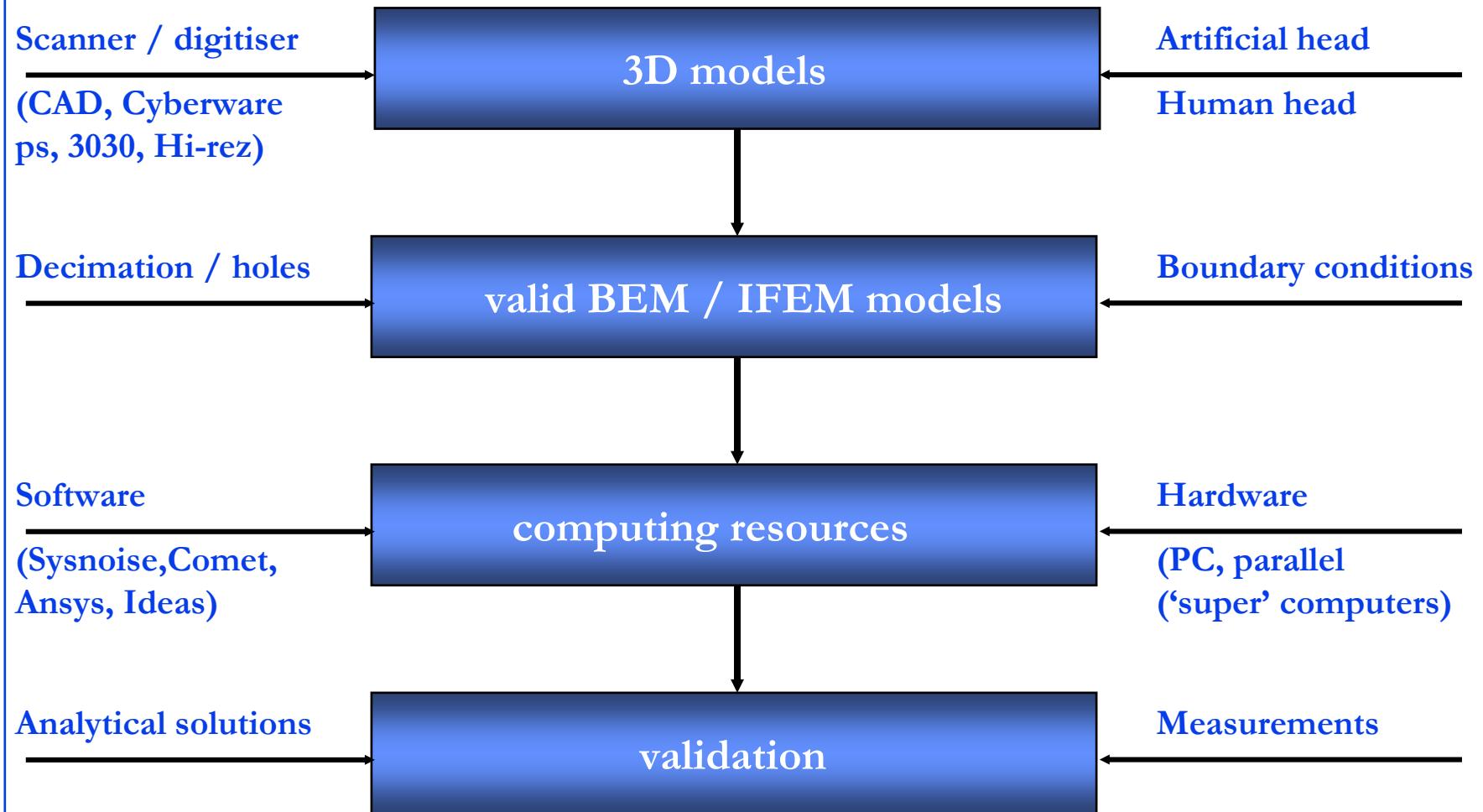
“Needless to say, this is analytically and computationally an intractable problem”

Also Genuit (1986), Katz (1998) and others using simplified techniques

CONTENTS

- Project description
- Overview of numerical modelling techniques in acoustics
- HRTFs and the principle of reciprocity (simple/complex models)
- Frequency response of baffled pinnae
- Acoustic modes of the external ear
- Spherical harmonics and mode shapes
- HRTFs extraction using the SVD and the BEM
- Sound field animations
- Conclusions

PROJECT “BOTTLE-NECKS”



NUMERICAL MODELLING OF HRTFs - OBJECTIVES

- Develop a tool for accurate analysis of the physical mechanisms of the external ear
- Analyse pinna-based spectral cues at high frequencies
- Obtain individualised HRTFs by means of an optical sensor
- Use numerical methods for analysis of simple models where analytical solutions cannot be used
- Visualise sound fields for virtual acoustic systems

Where are we?

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METHODS FOR ACOUSTIC CALCULATIONS

Analytical methods

- Closed form solutions
- Only for simple geometry

Geometrical methods

- Ray/beam tracing
- Mirror images

Statistical energy methods (SEA)

- Energy exchanges between system components

Numerical methods

- Finite Element Method (FEM)
 - Volume discretisation into finite elements
- Boundary Element Method (BEM)
 - Discretisation of bounding surface into boundary elements

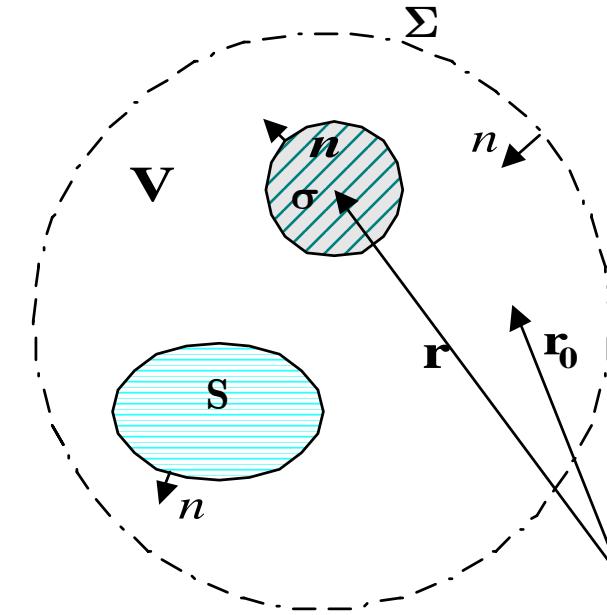
BEM - DIRECT BOUNDARY INTEGRAL EQUATION (BIE)

Inhomogeneous Helmholtz equation (harmonic excitation)

$$(\nabla^2 + k^2)p(\mathbf{r}) = -Q_{\text{vol}}(\mathbf{r}_0)$$

Free space Green function

$$g(\mathbf{r} | \mathbf{r}_0) = \frac{e^{-jk|\mathbf{r}-\mathbf{r}_0|}}{4\pi |\mathbf{r} - \mathbf{r}_0|}$$



$$p(\mathbf{r}) = \int_S [g(\mathbf{r} | \mathbf{r}_0) \nabla_0 p(\mathbf{r}_0) - p(\mathbf{r}_0) \nabla_0 g(\mathbf{r} | \mathbf{r}_0)] \cdot \mathbf{n} dS$$

3D $\sum \rightarrow$ 2D - computationally inefficient

BEM - PROPERTIES

DBEM (Direct BEM)

- Solves the pressure and particle velocity on the boundary surface
- Exterior *or* interior domains
- Discretisation, collocation, shape functions, nonsymmetric matrices
- Efficient with small to medium size problems

IBEM (Indirect BEM)

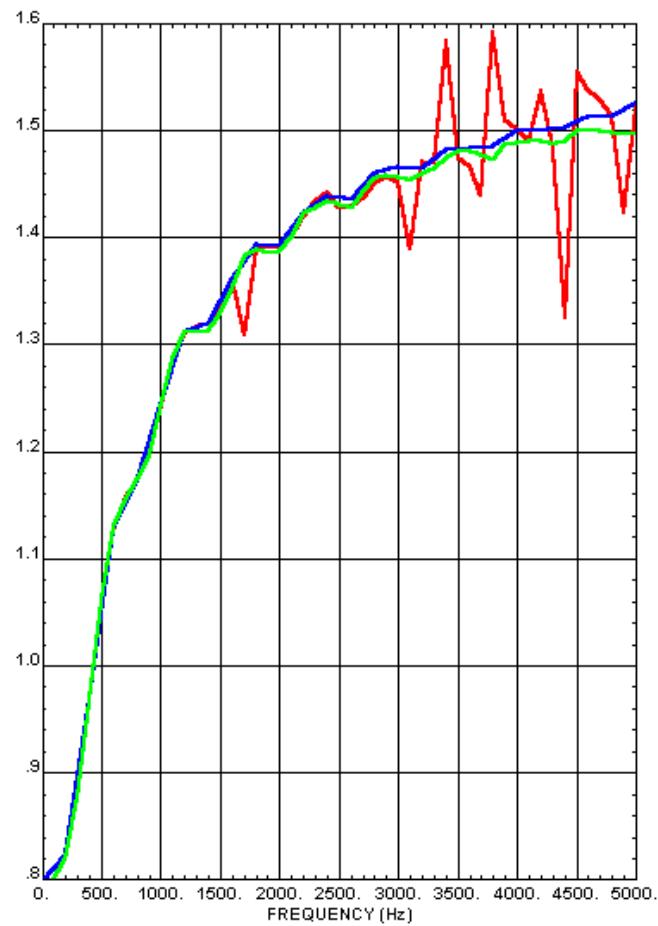
- Solves the differences between the outside and inside values of the pressure and particle velocity on the boundary surface
- Exterior *and* interior domains
- Variational formulation, symmetric matrices
- Efficient with large problems

Special formulation: symmetric, axisymmetric, baffled models

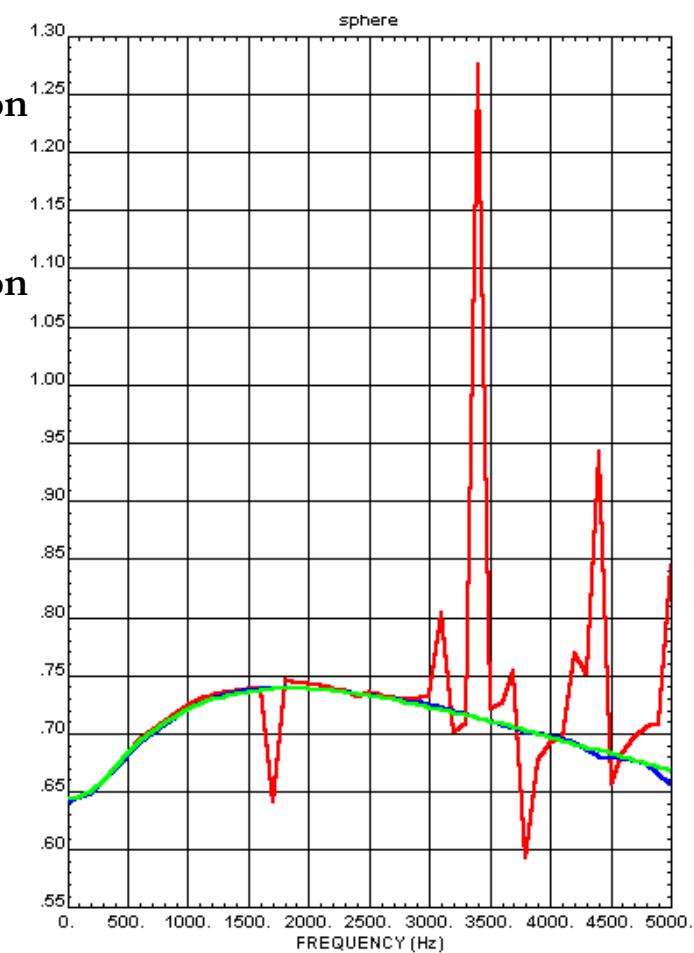
Non-uniqueness problem (irregular frequencies) $\sum \rightarrow$ regularisation

THE “NON-UNIQUENESS” PROBLEM VALIDATION OF THE SPHERE MODEL

Front



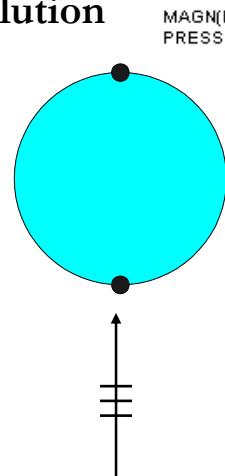
Rear



With
overdetermination

Without
overdetermination

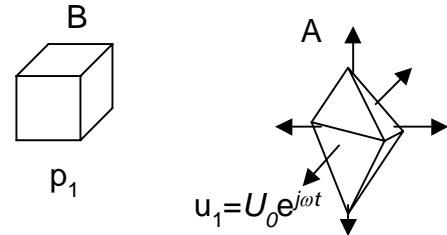
Analytical
solution



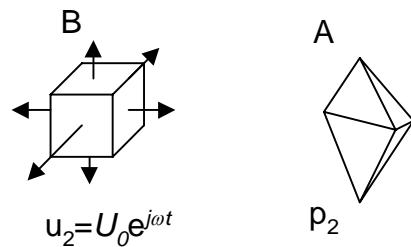
Where are we?

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CALCULATION OF HRTFs USING THE PRINCIPLE OF RECIPROCITY

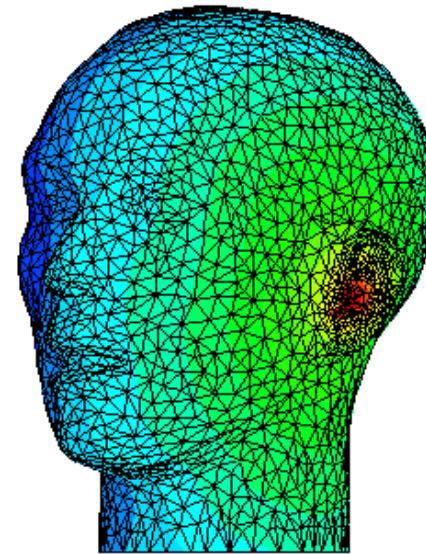


$$\oint_S (\mathbf{p}_1 \vec{\mathbf{u}}_2 - \mathbf{p}_2 \vec{\mathbf{u}}_1) \cdot \hat{\mathbf{n}} dS = 0$$

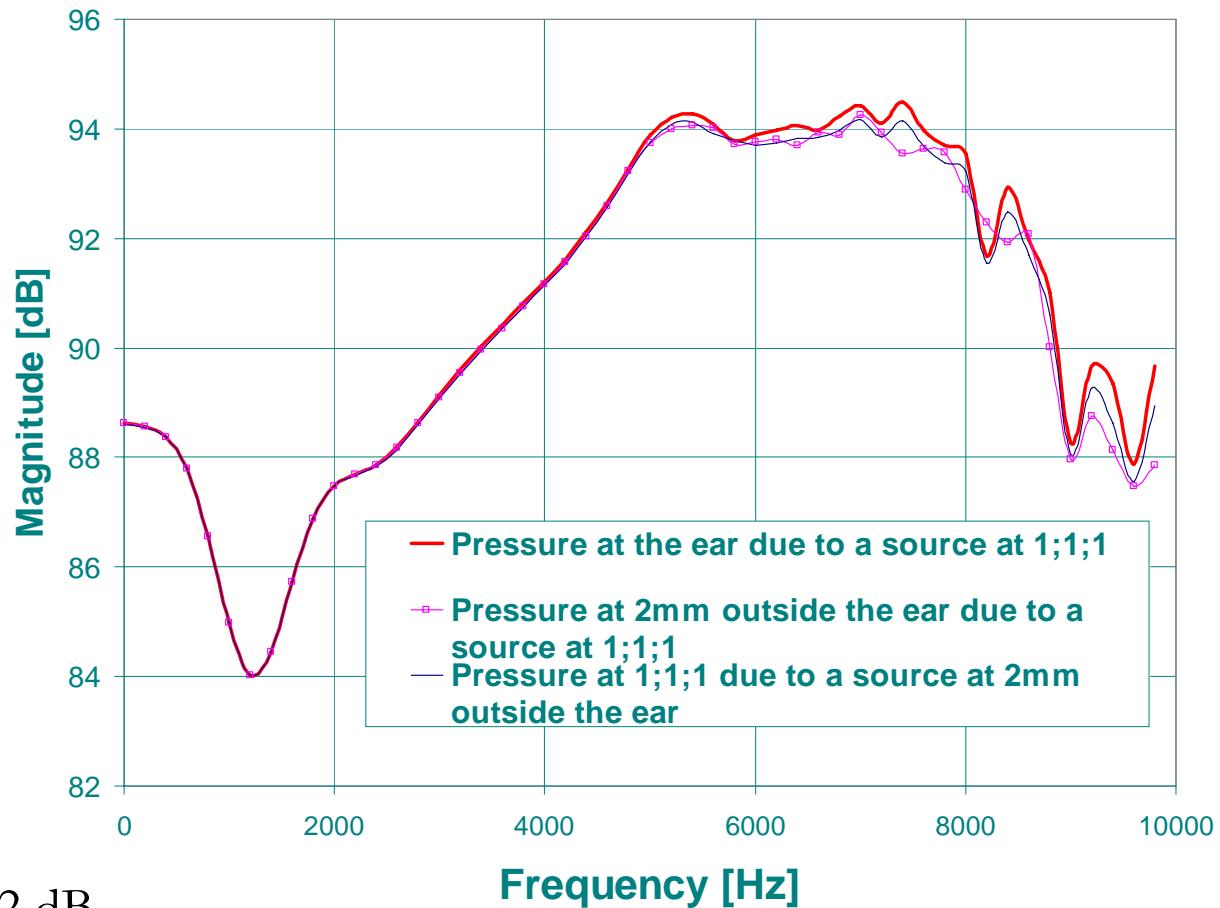


$$\frac{Q_1}{P_1(r)} = \frac{Q_2}{P_2(r)}$$

- Refined ear
- Source positioned close to entrance to ear-canal

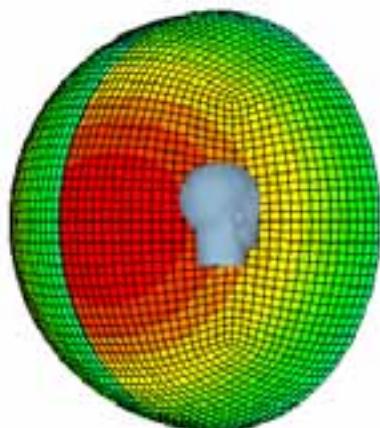


VALIDATION OF THE PRINCIPLE OF RECIPROCITY

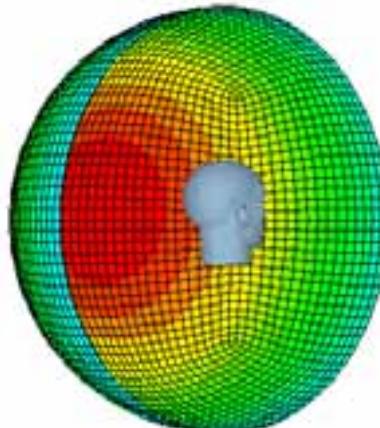


- Errors: <0.2 dB
- HRTFs can be calculated with high accuracy for near-field and far-field

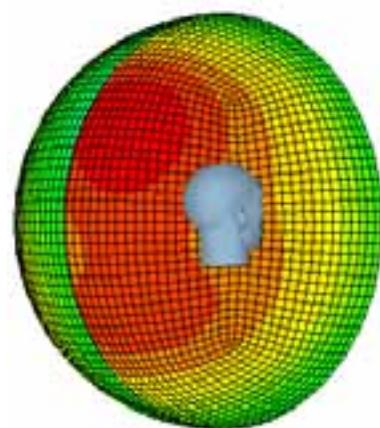
CALCULATION OF HRTFs USING THE PRINCIPLE OF RECIPROCITY (dB scale)



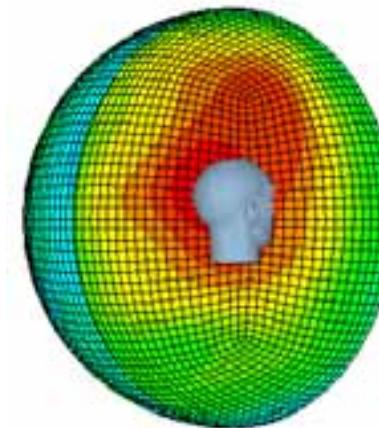
-2.3 / +2.7



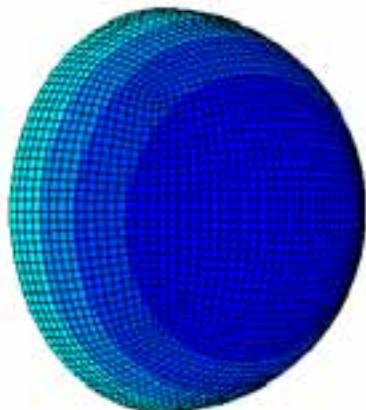
-7.2 / +7.2



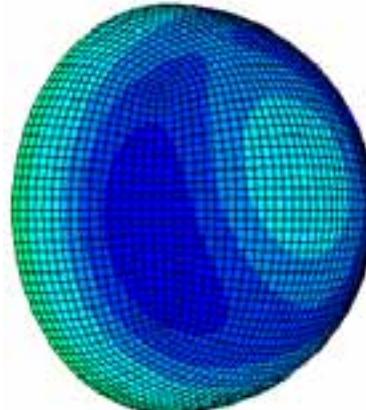
-32.7 / +8.3



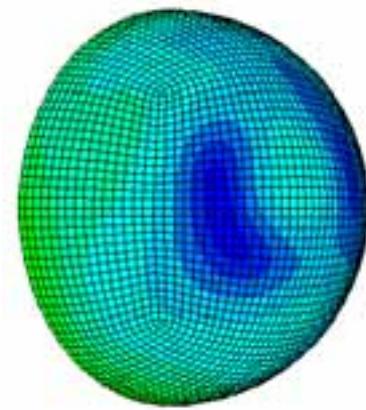
-39 / +16.5



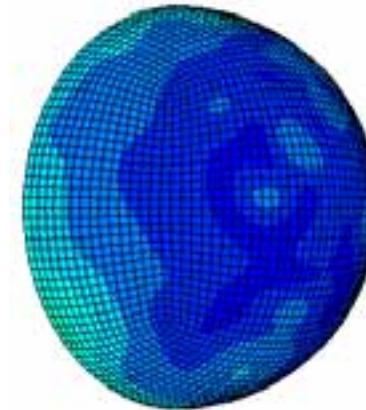
200 Hz



1,000 Hz



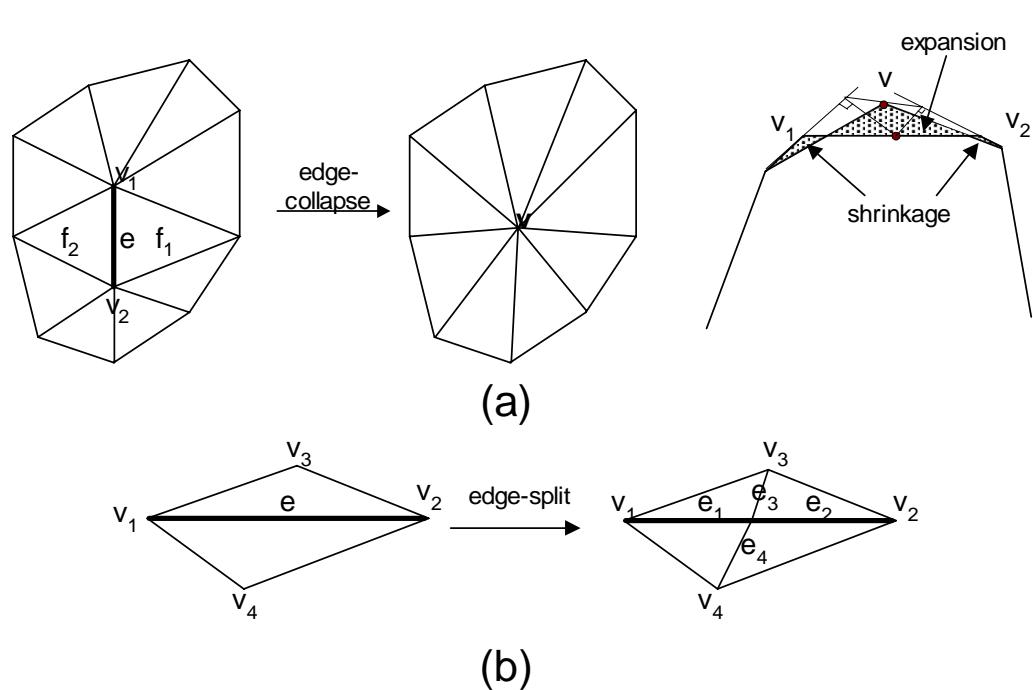
2,000 Hz



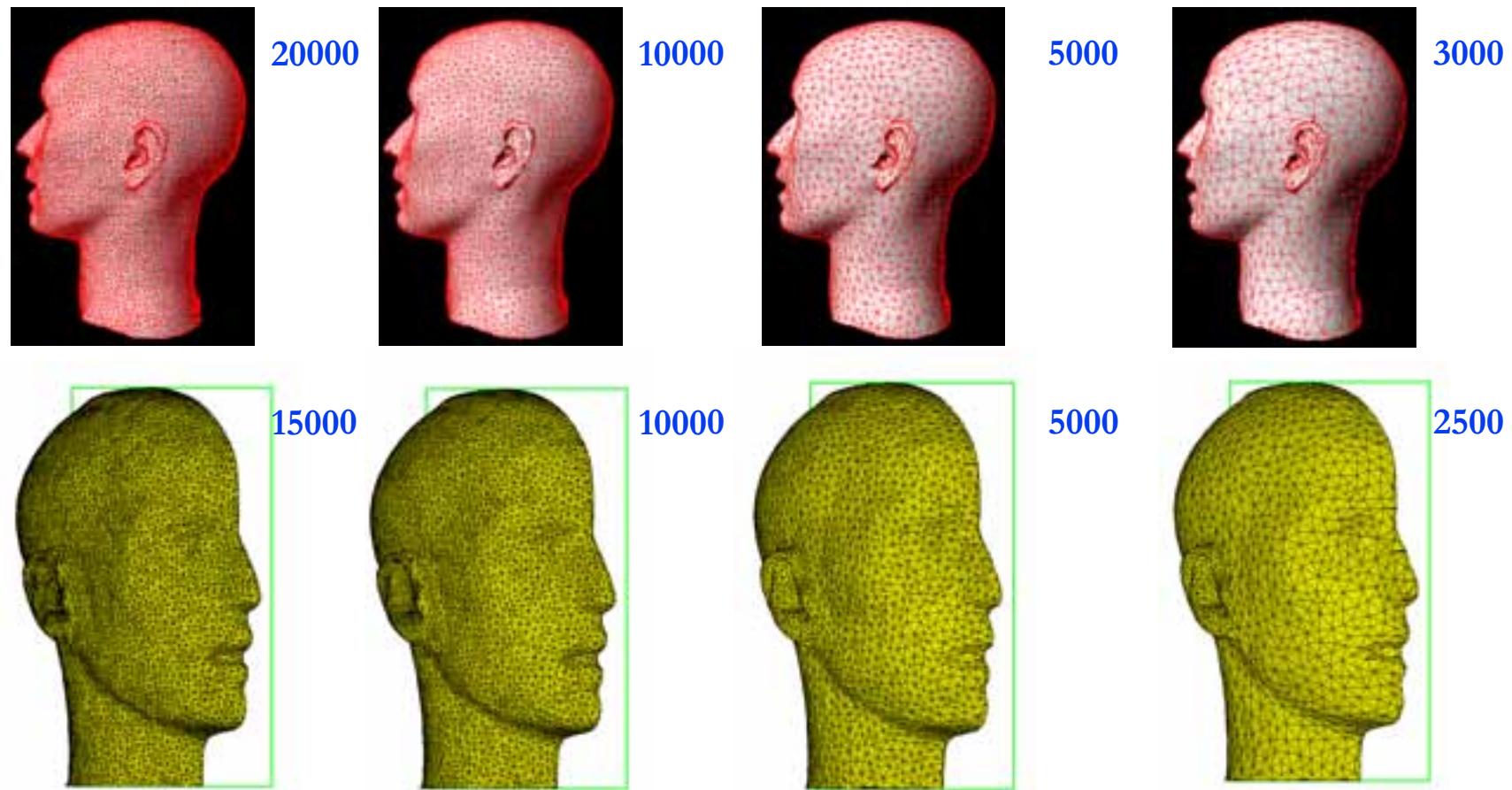
5,000 Hz

MESH DECIMATION

- Preserve shape
- Normalise distances between vertices
- Minimise number of vertices
- Edge split, edge collapse



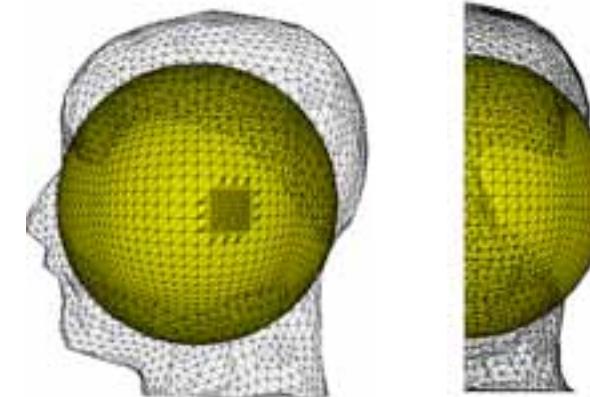
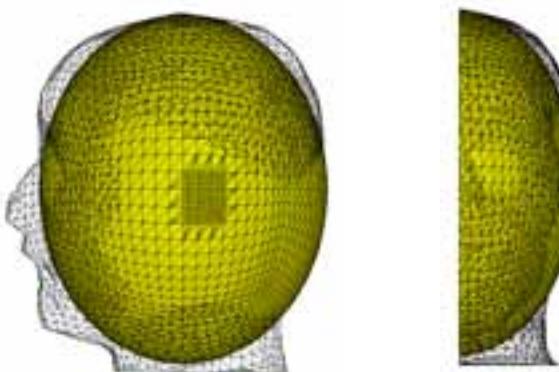
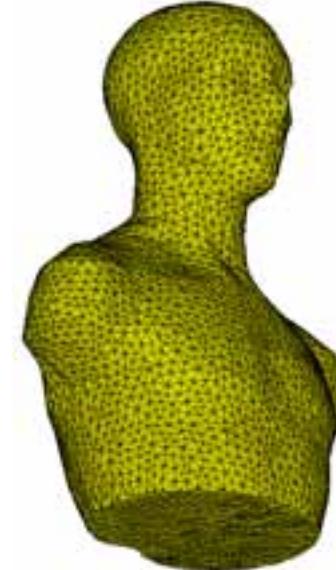
POLYGON REDUCTION / NORMALISED MESH MODELS - FULL AND HALF MODELS OF KEMAR



No. of elements

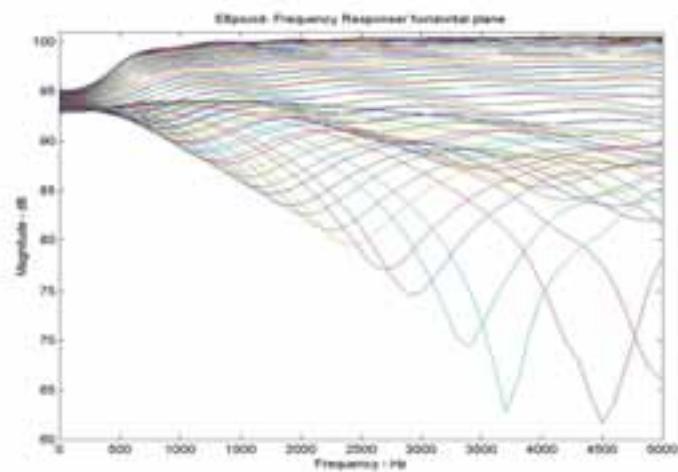
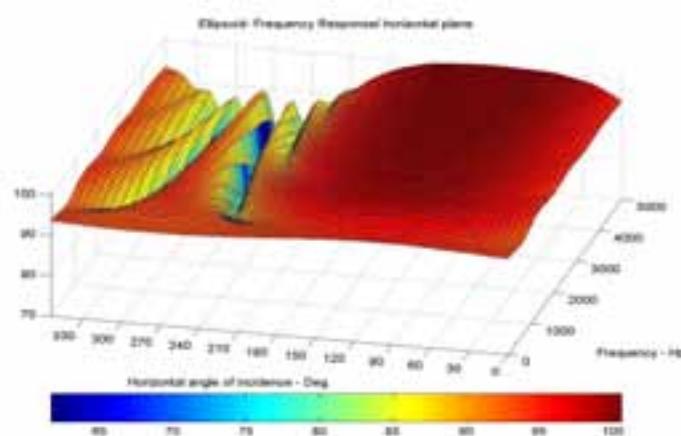
HRTF SIMULATION OF LOW-MEDIUM SIZE SIMPLE MODELS

- CORTEX head - with and without torso.
Converted from CAD and decimated.
- Sphere - $r = 8.75 \text{ [cm]}$
- Ellipsoid - $r_x = 9.6, r_y = 7.9, r_z = 11.6 \text{ [cm]}$.
- ‘Ear’ positions optimised for minimal errors, and locally refined for reciprocity.

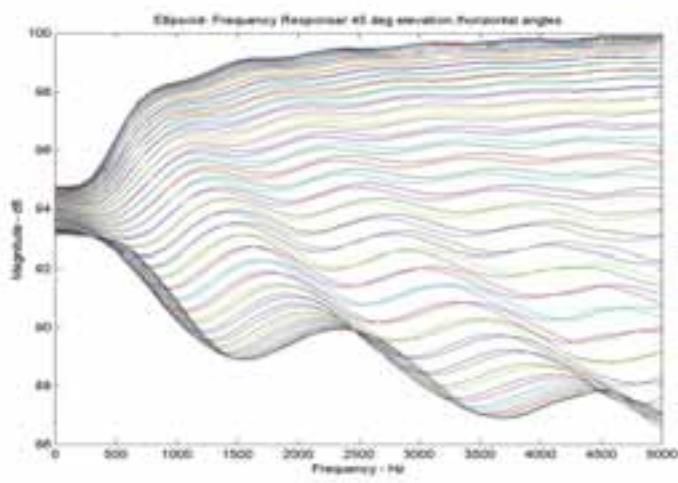
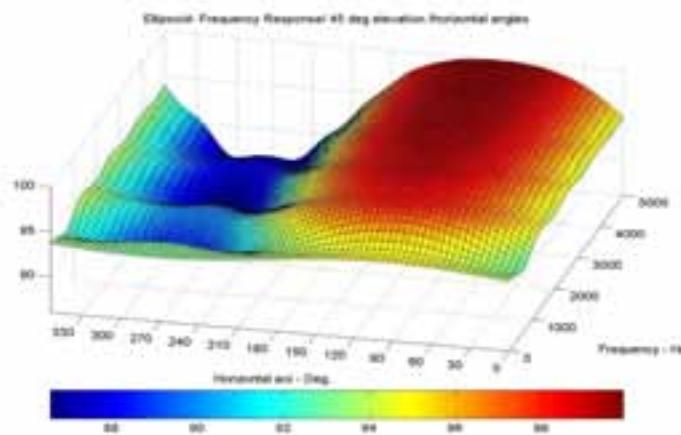


HRTFs OF AN ELLIPSOID

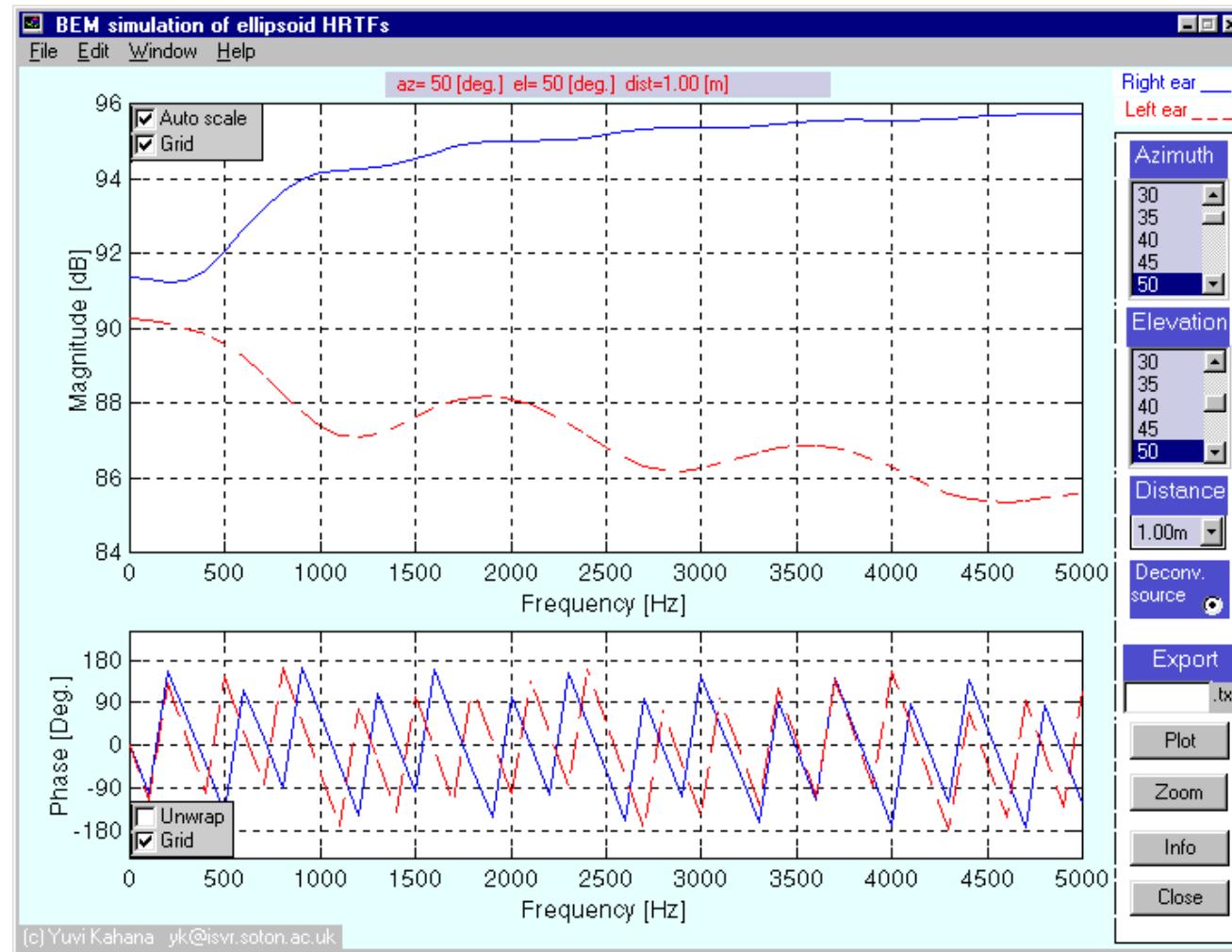
HRTFs at horizontal plane ($el = 0^\circ, \alpha\zeta = 0^\circ - 355^\circ$)

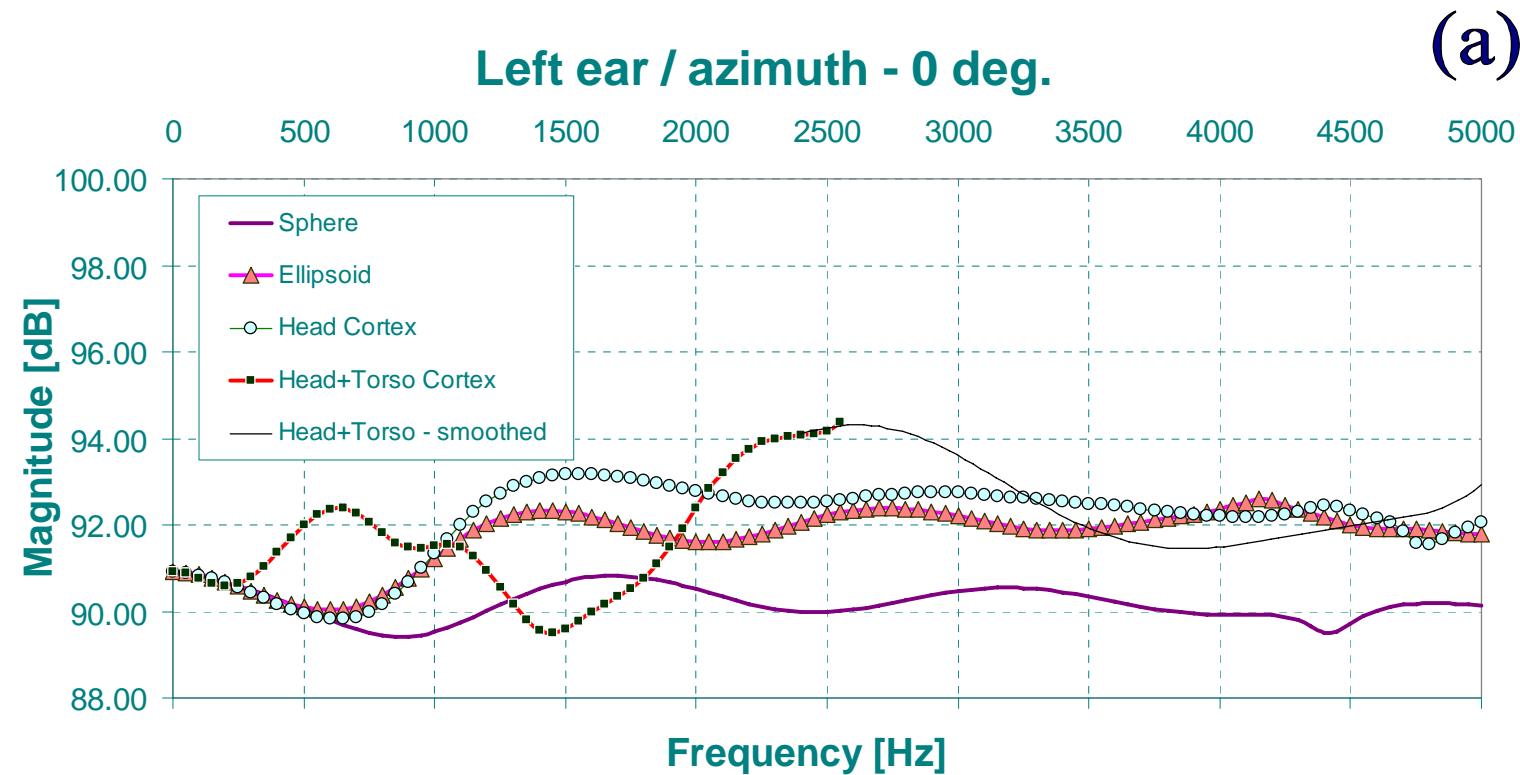


HRTFs at elevation ($el = 45^\circ, \alpha\zeta = 0^\circ - 355^\circ$)



MATLAB GUI OF NUMERICALLY MODELLED HRTFs OF AN ELLIPSOID

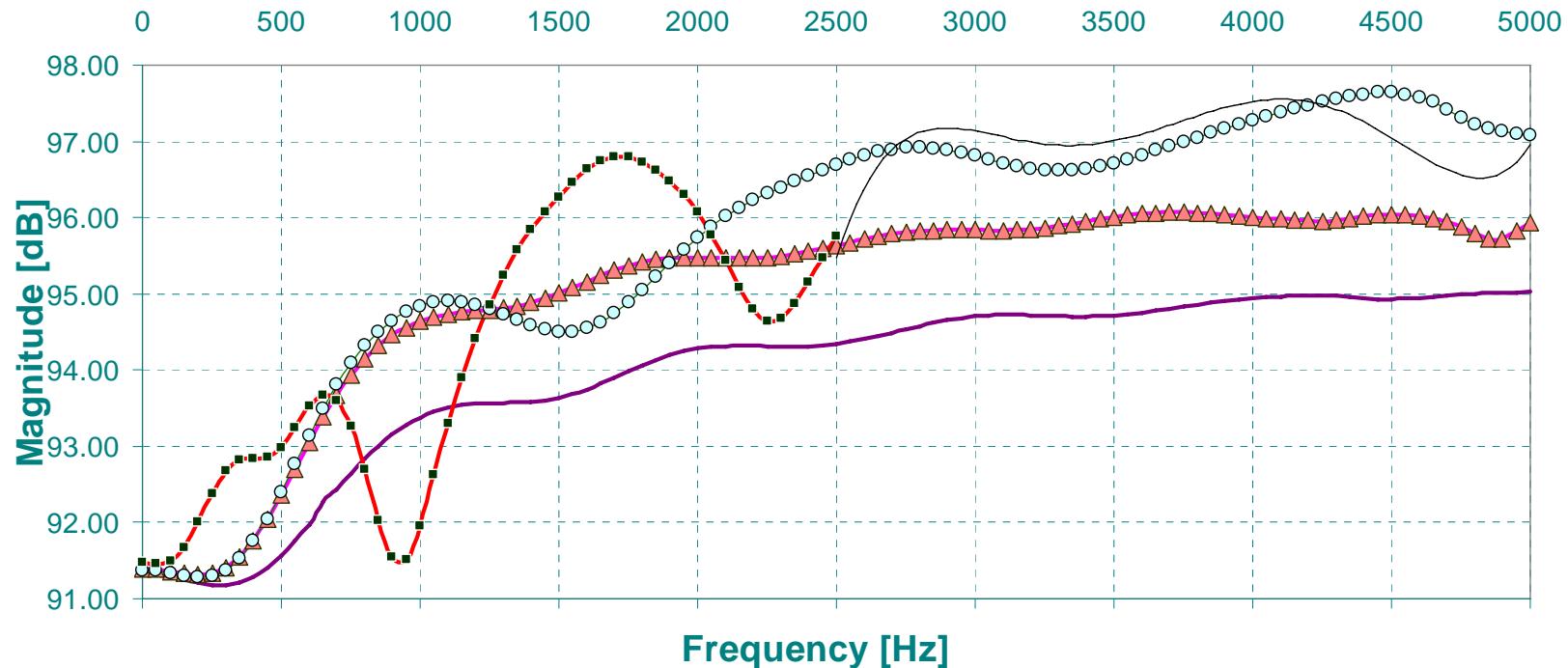


COMPARISON OF HRTFs OF SIMPLE MODELS-
HORIZONTAL PLANE

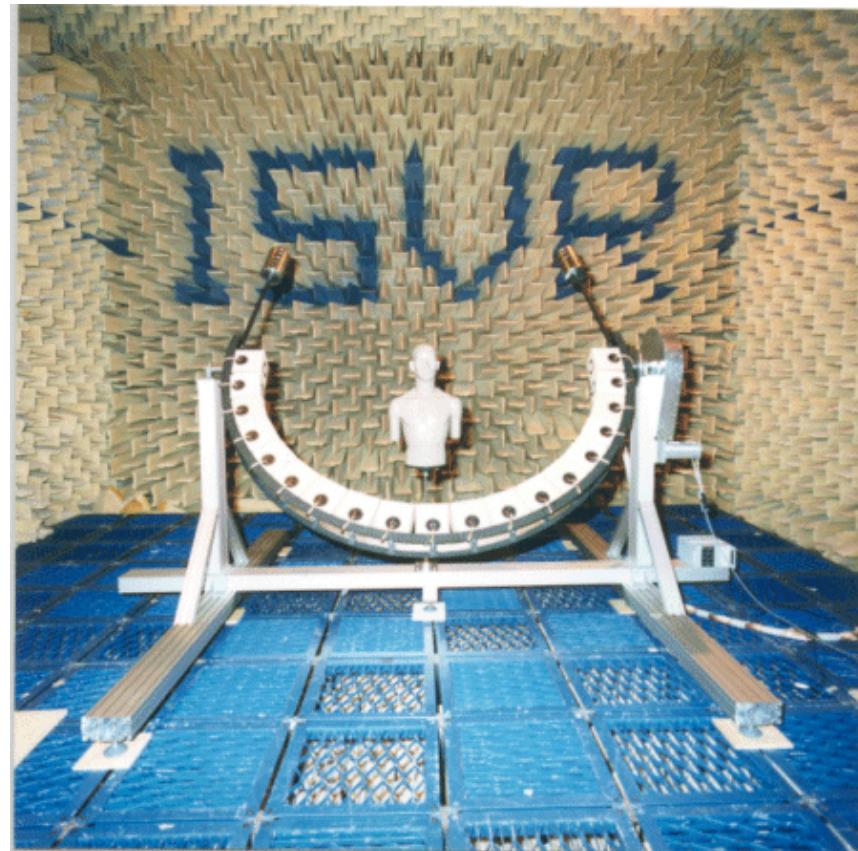
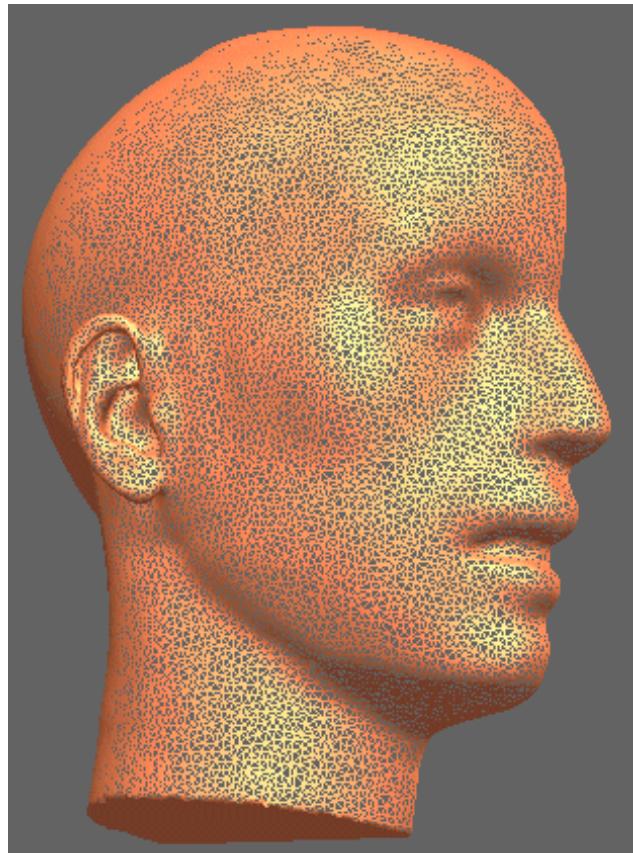
COMPARISON OF HRTFs OF SIMPLE MODELS -
AT ELEVATION

(e)

Right ear /azimuth 45 deg./elev 45 deg.

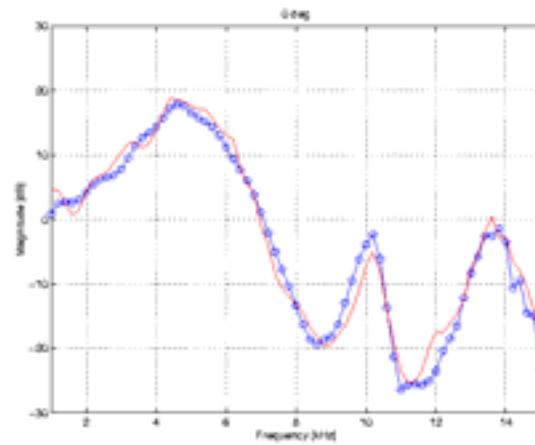


HRTF SIMULATION AND MEASUREMENT ARRANGEMENTS

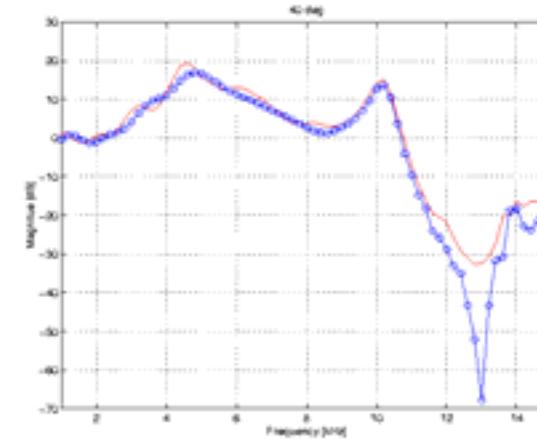
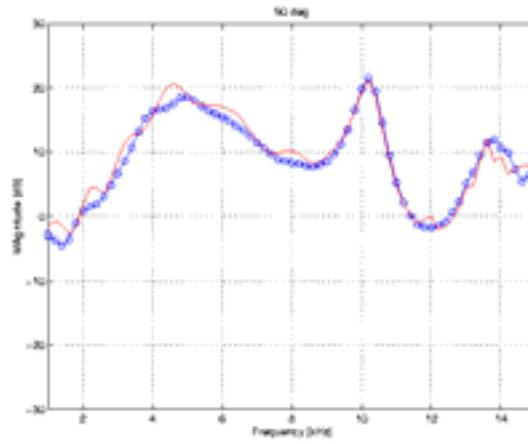


HRTFs OF KEMAR (WITH DB60) MEDIAN PLANE MEASUREMENT AND SIMULATION

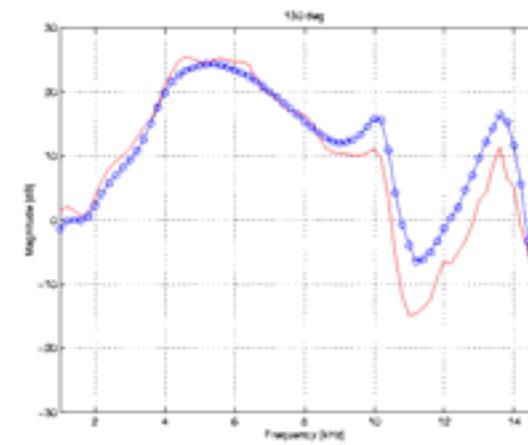
0 deg. 40 deg.



90 deg.

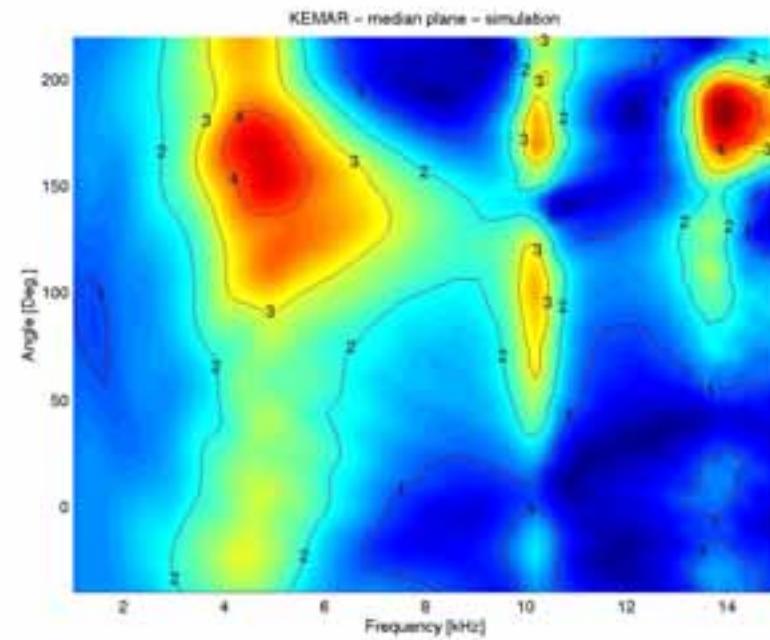


130 deg.

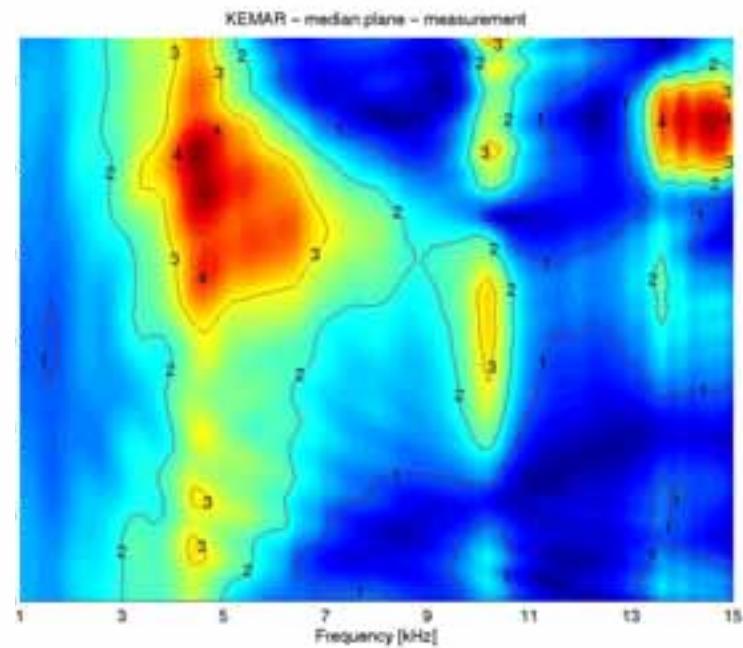


COLOUR MAPS OF SIMULATION AND MEASUREMENT OF THE HRTFs OF KEMAR - MEDIAN PLANE

SIMULATION

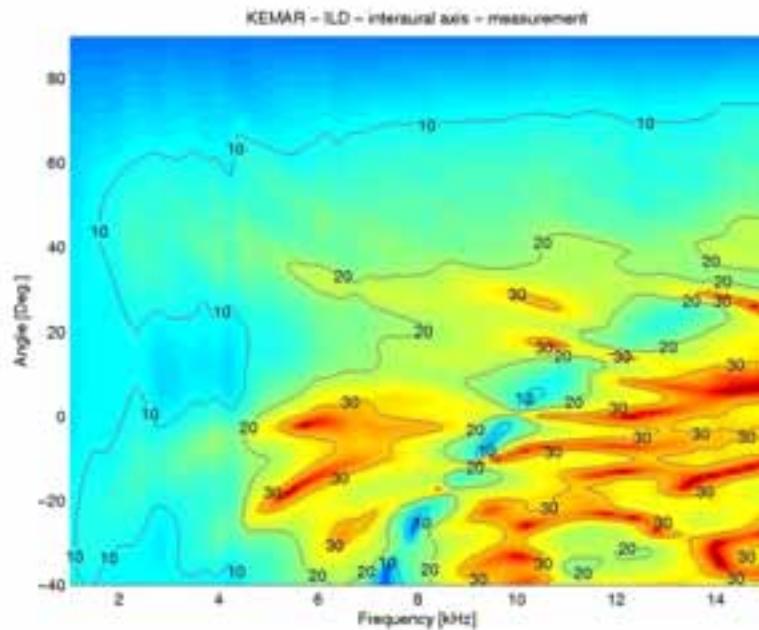


MEASUREMENT

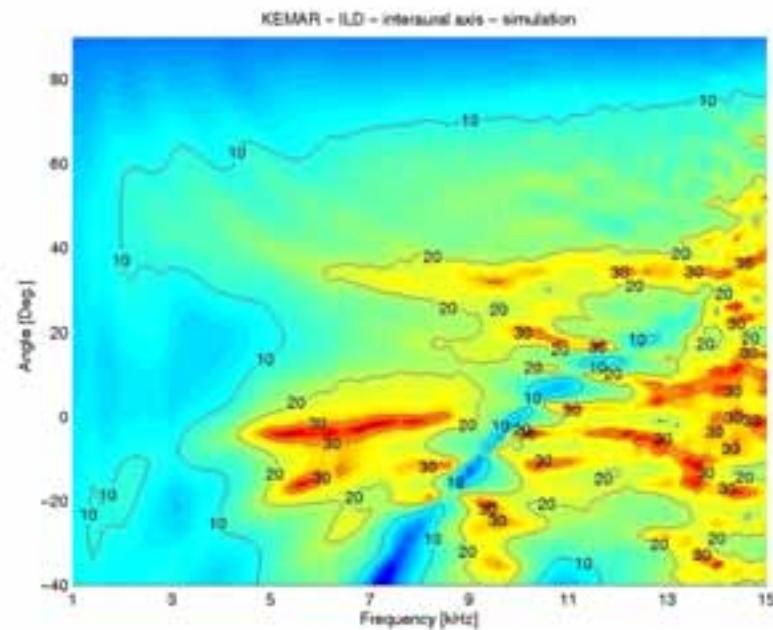


COMPARISON OF SIMULATION AND MEASUREMENT OF THE ILD IN THE LATERAL VERTICAL PLANE

SIMULATION



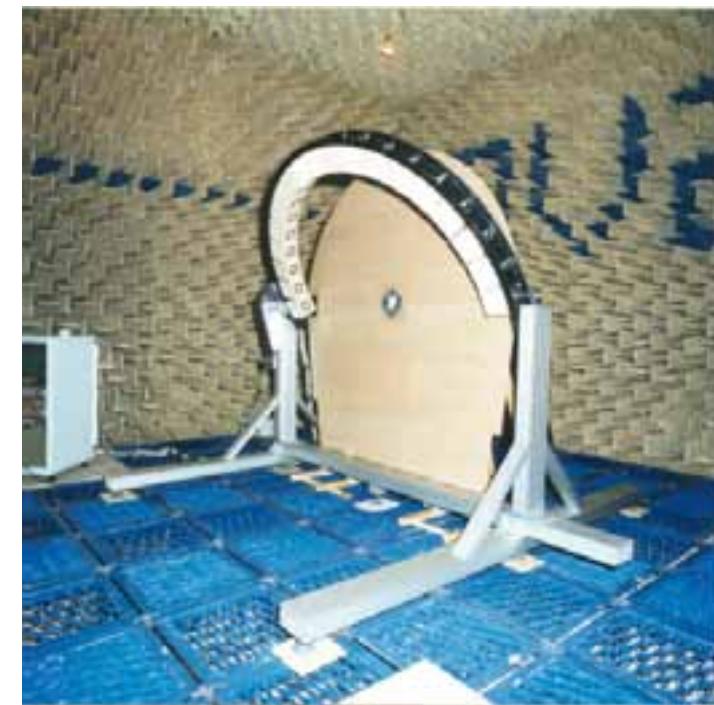
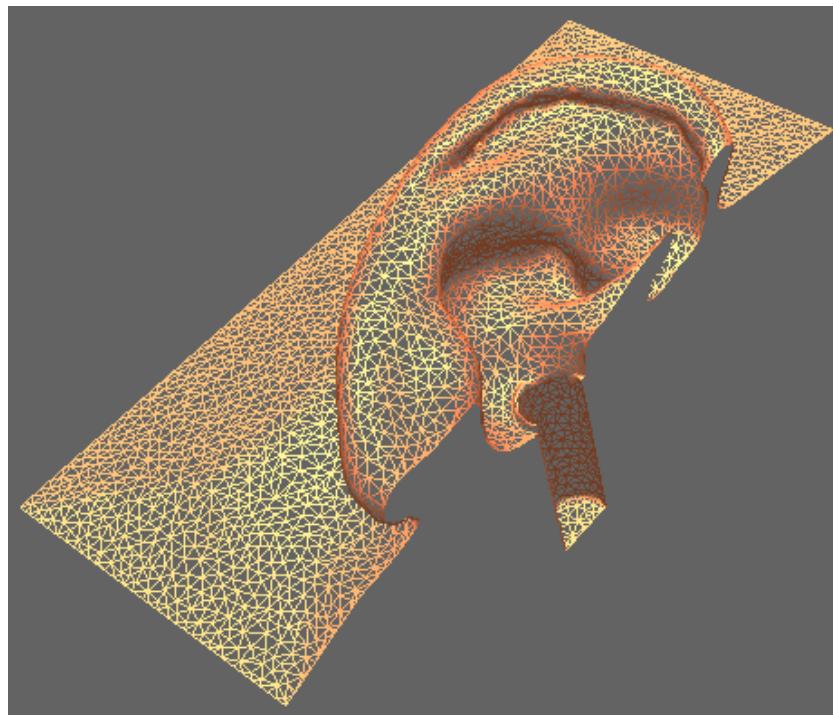
MEASUREMENT



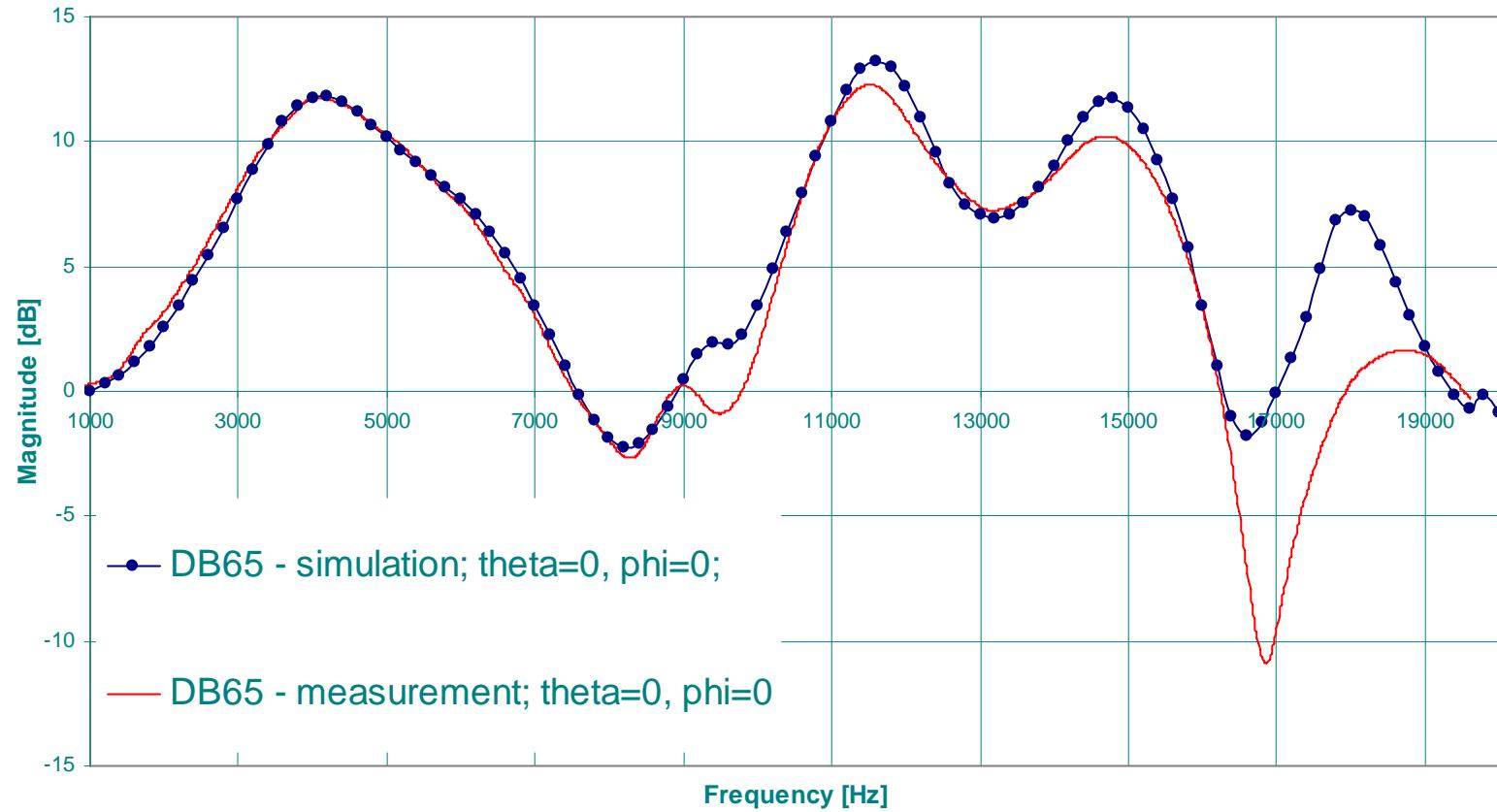
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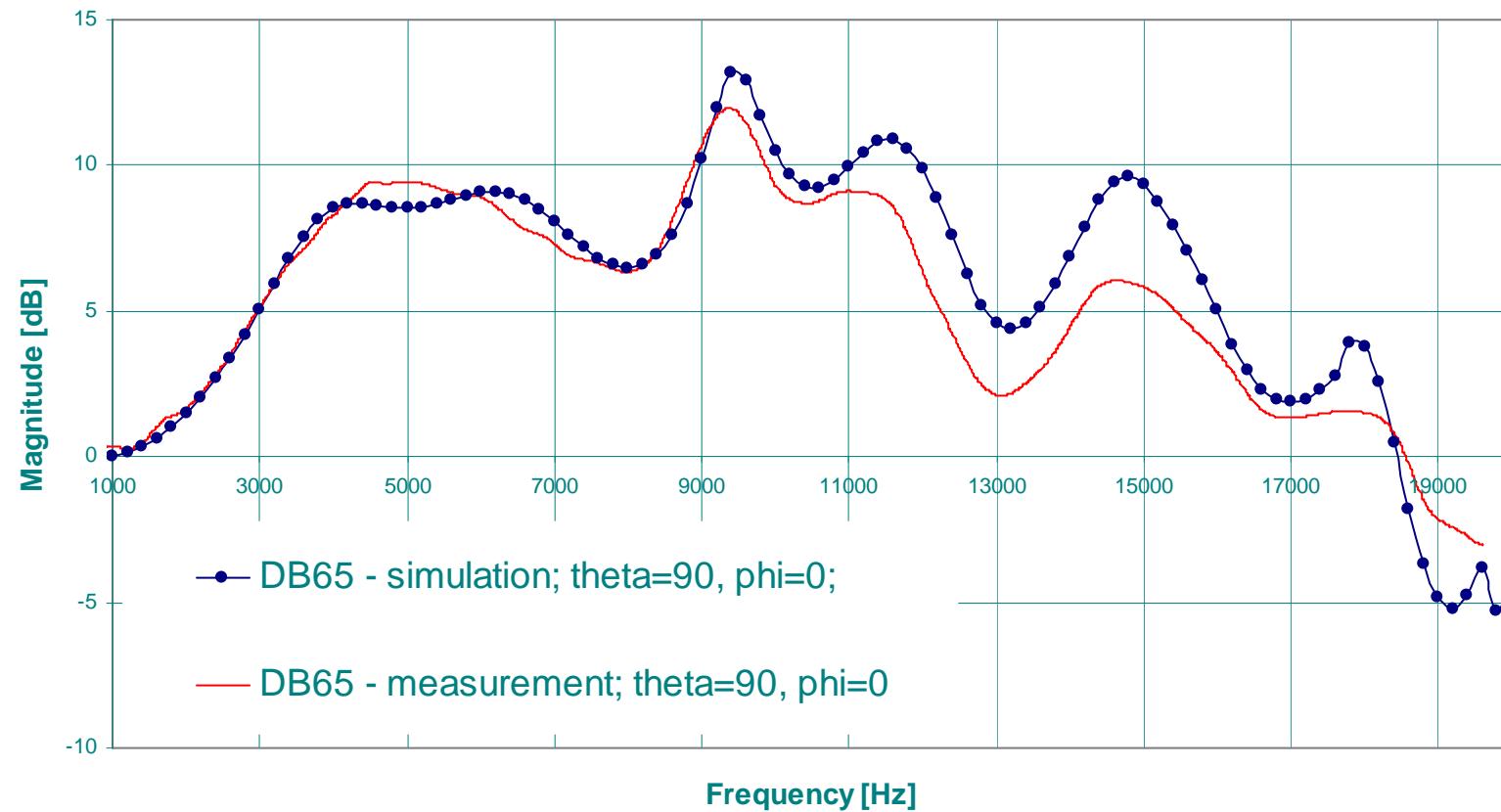
THE RESPONSE OF THE EXTERNAL EAR - SIMULATION MODEL AND MEASUREMENT APPARATUS



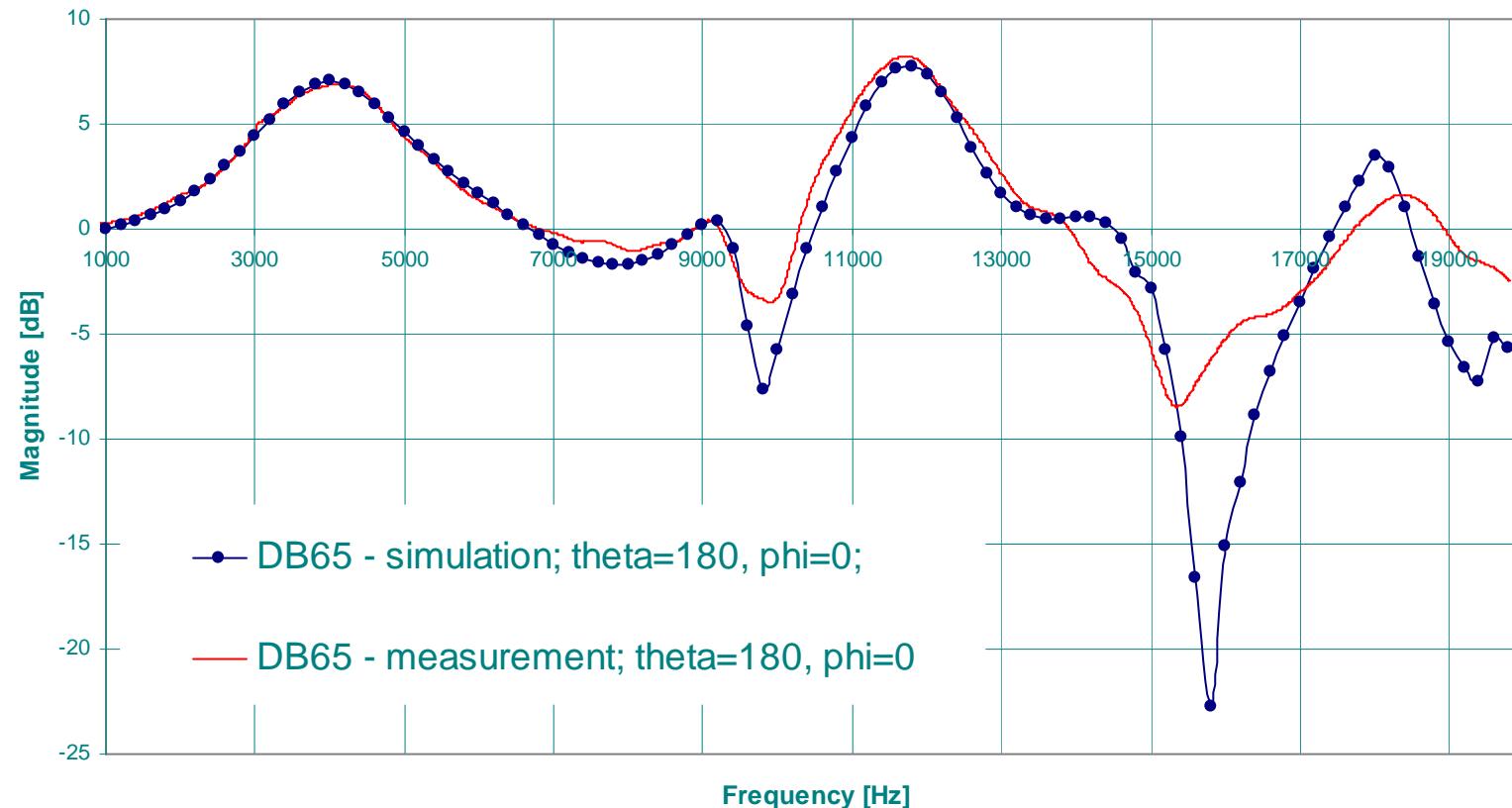
SIMULATION AND MEASUREMENT OF THE RESPONSE OF A BAFFLED DB65 PINNA - $\theta=0$



SIMULATION AND MEASUREMENT OF THE RESPONSE OF A BAFFLED DB65 PINNA - $\theta=90$

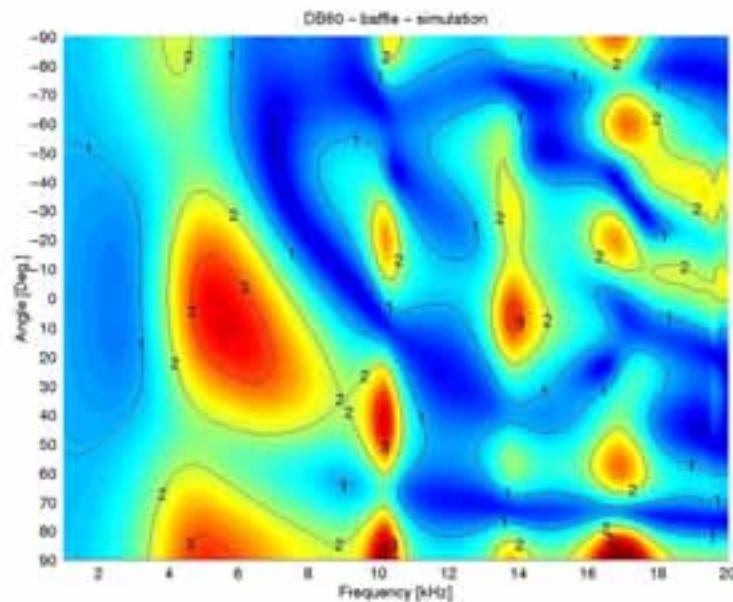


SIMULATION AND MEASUREMENT OF THE RESPONSE OF A BAFFLED DB65 PINNA - $\theta=180$

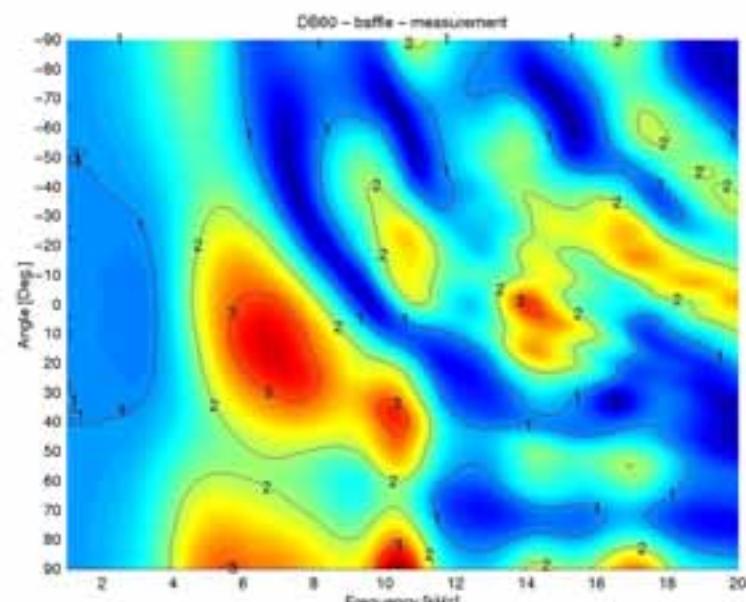


SIMULATION AND MEASUREMENT OF THE RESPONSE OF A BAFFLED DB60 PINNA

SIMULATION



MEASUREMENT

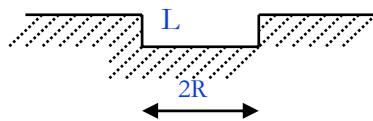


- Lateral vertical (frontal) plane
- Resolution of 1 degree on a linear scale
- High accuracy up to 20 kHz

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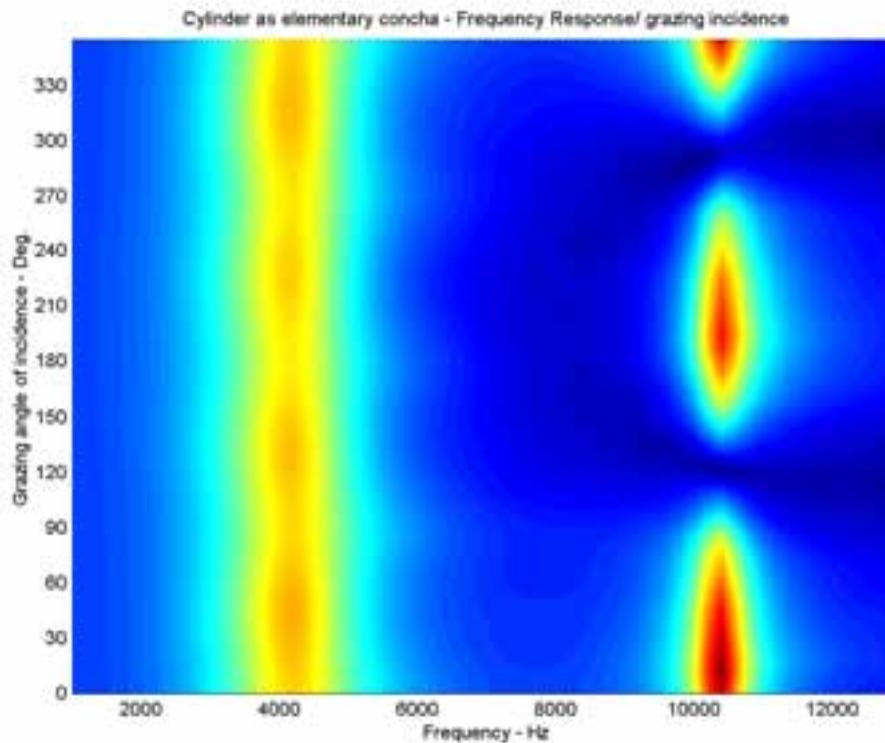
MODES OF A CYLINDER IN AN INFINITE BAFFLE



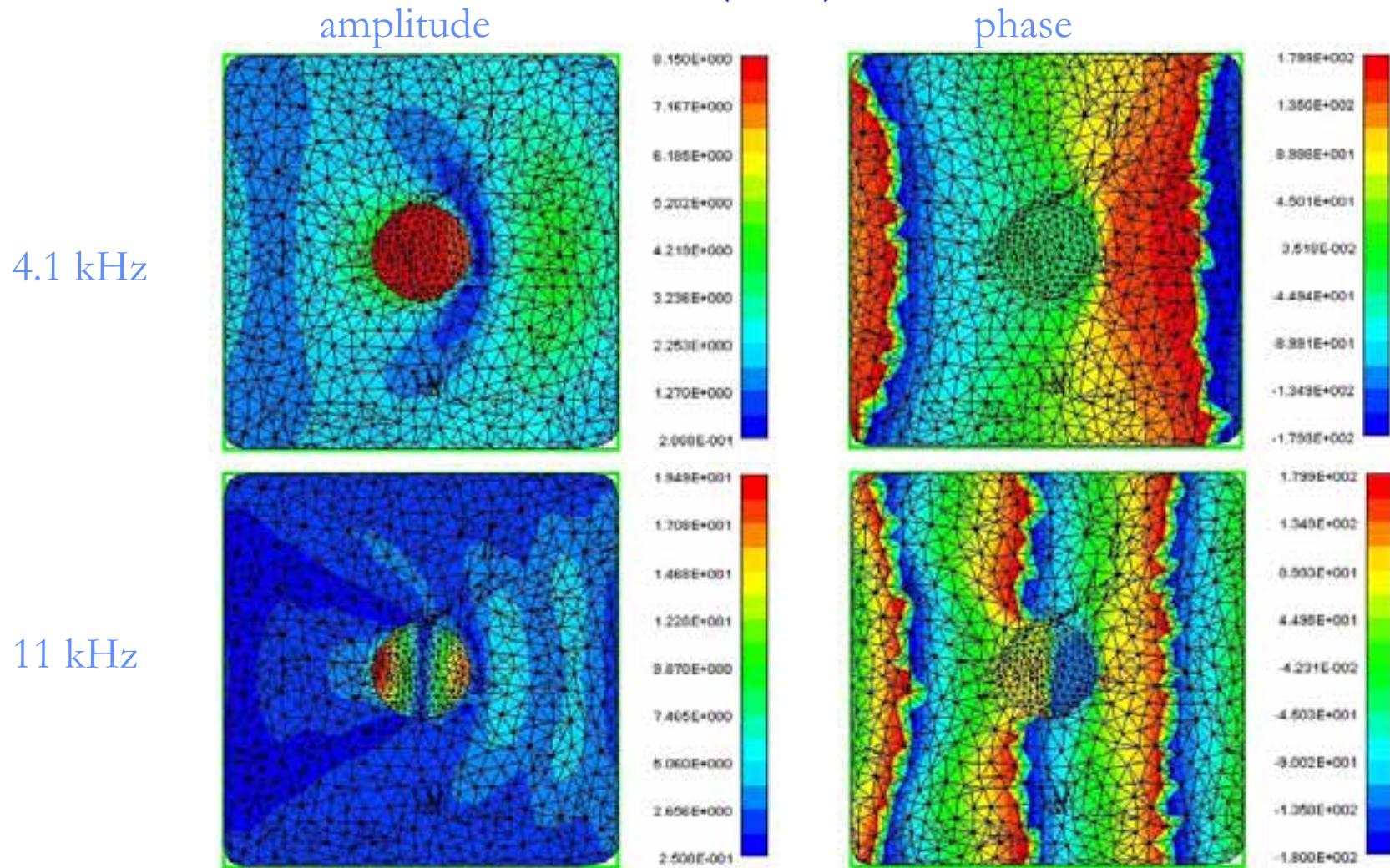
L=10mm, 2R=22mm

- Simple theory

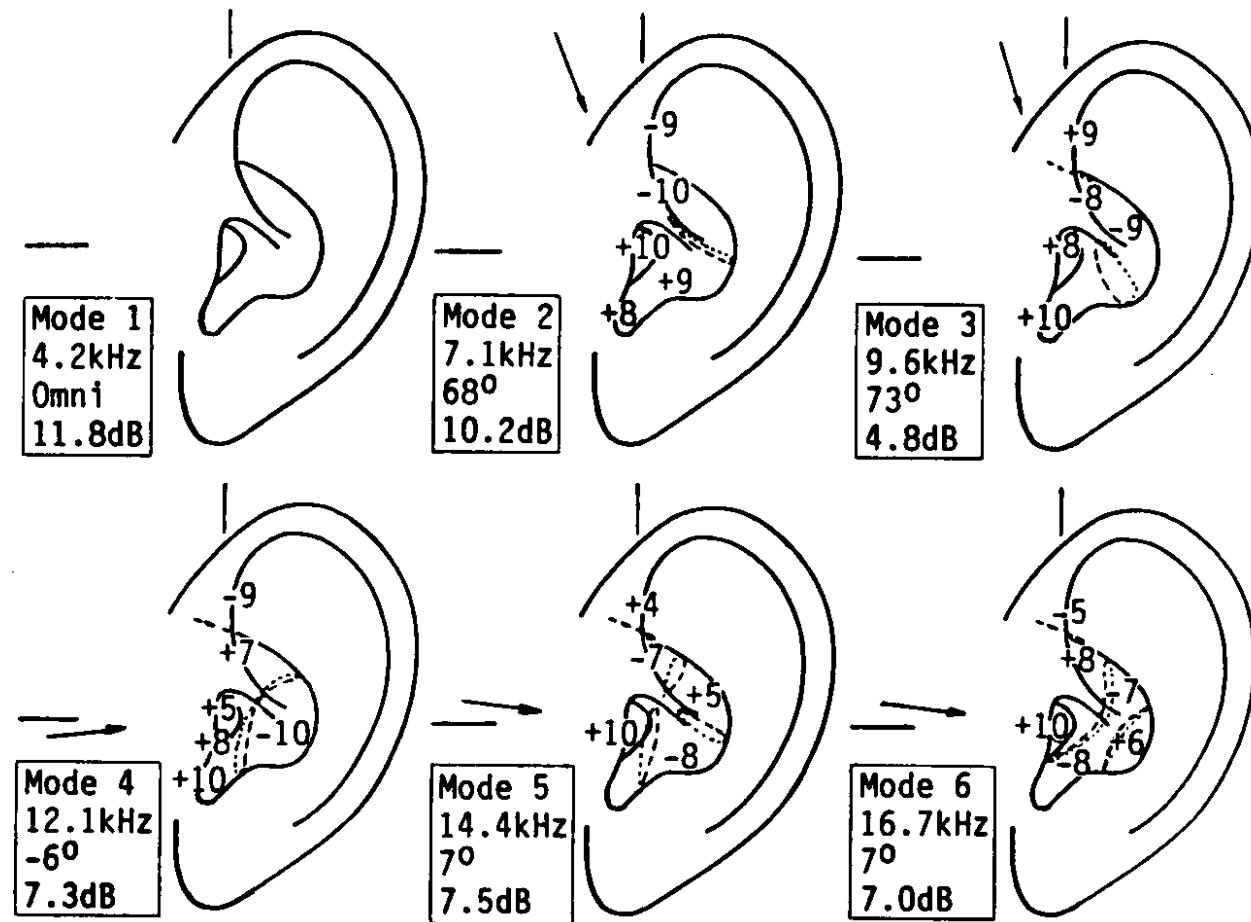
$$\left\{ \begin{array}{l} \frac{\lambda_{\max}}{4R} = \frac{L}{R} + 0.822 \\ \frac{P}{P_0} = 1 + 7.86 \left(\frac{L}{R} \right) \text{ [dB]} \end{array} \right.$$



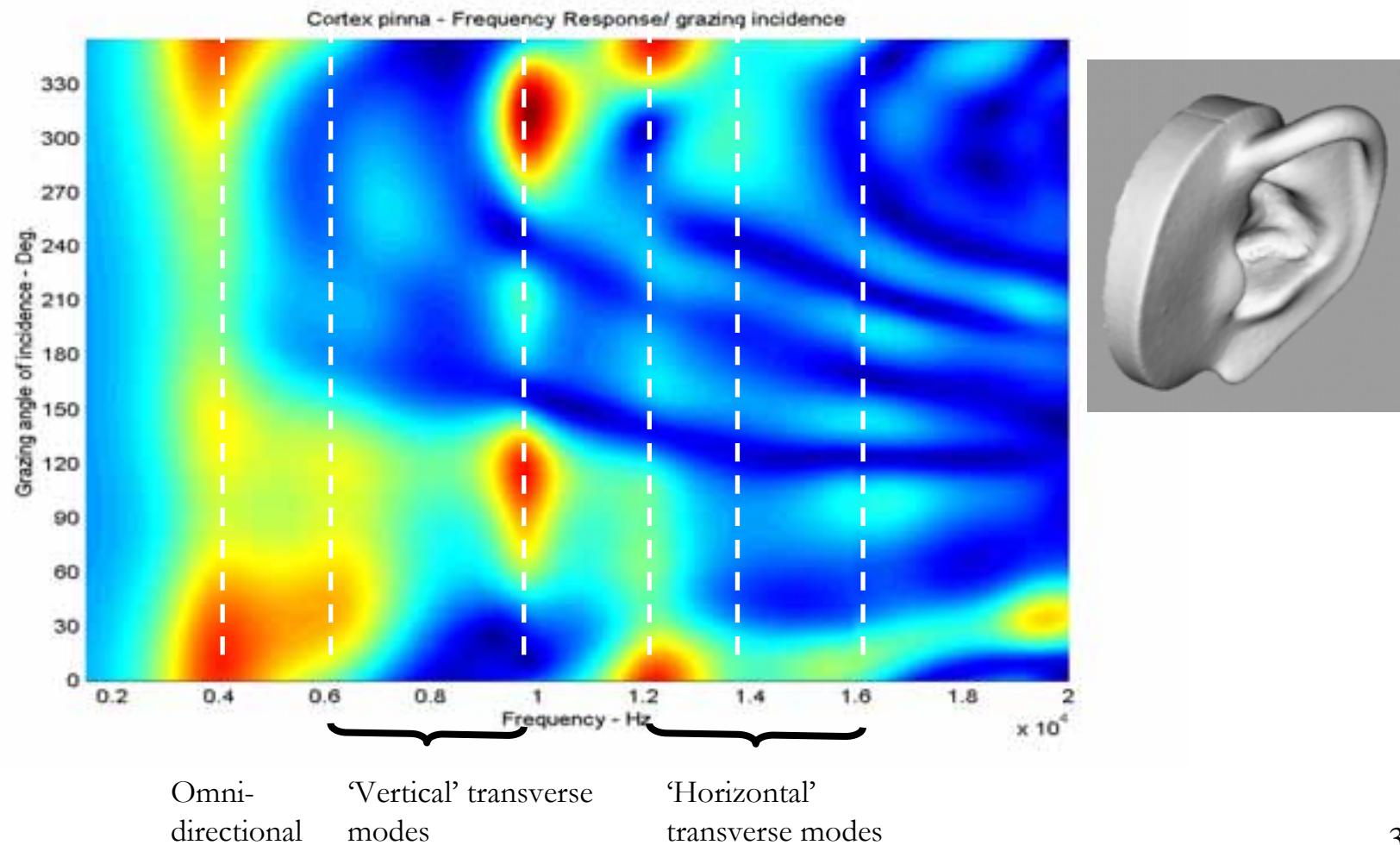
MODES OF AN INCLINED CYLINDER IN AN INFINITE BAFFLE (cont.)



MODE SHAPES OF THE EXTERNAL EAR (AVERGAE OF 10 PINNAE) EXCITATION AT GRAZING INCIDENCE (AFTER SHAW 1997)

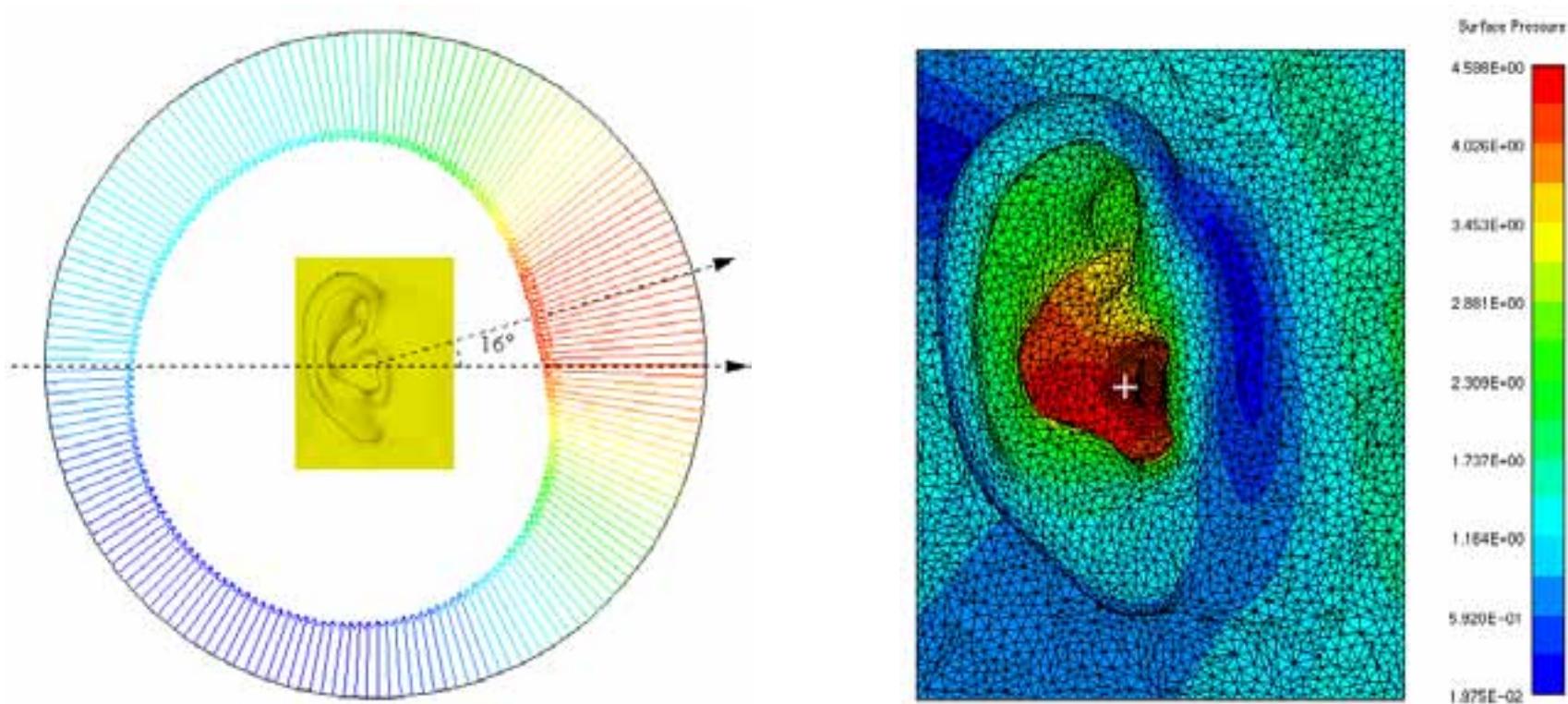


FREQUENCY RESPONSE OF THE CORTEX PINNA IN AN INFINITE BAFFLE - GRAZING INCIDENCE ANGLES



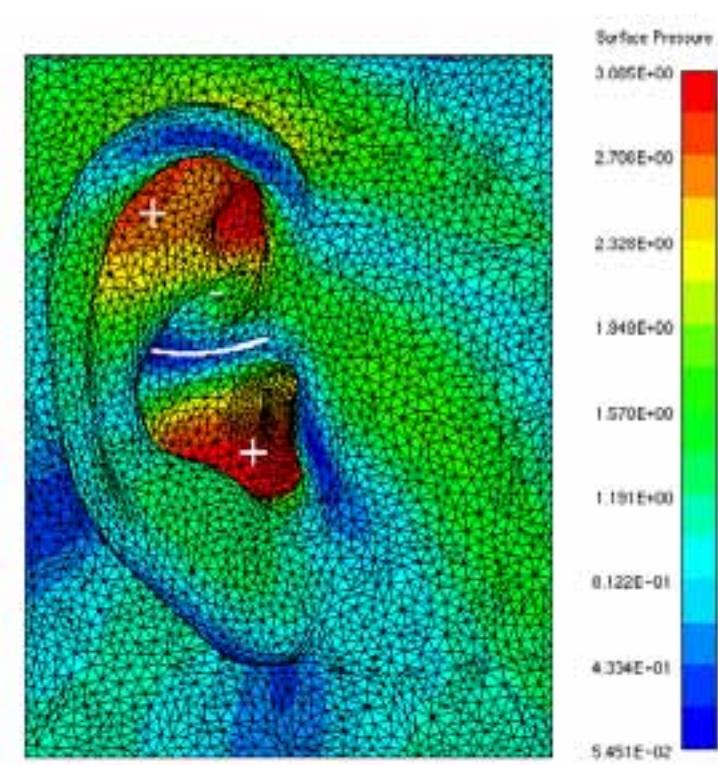
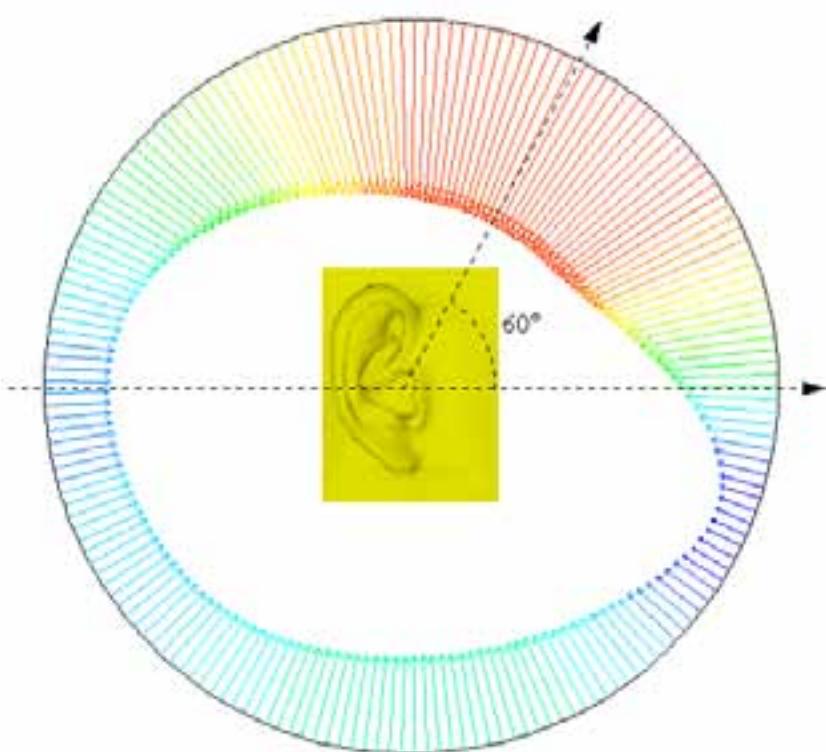
BEM SIMULATION OF THE MODE SHAPES OF THE DB65 PINNA –THE FIRST MODE

4.2 kHz



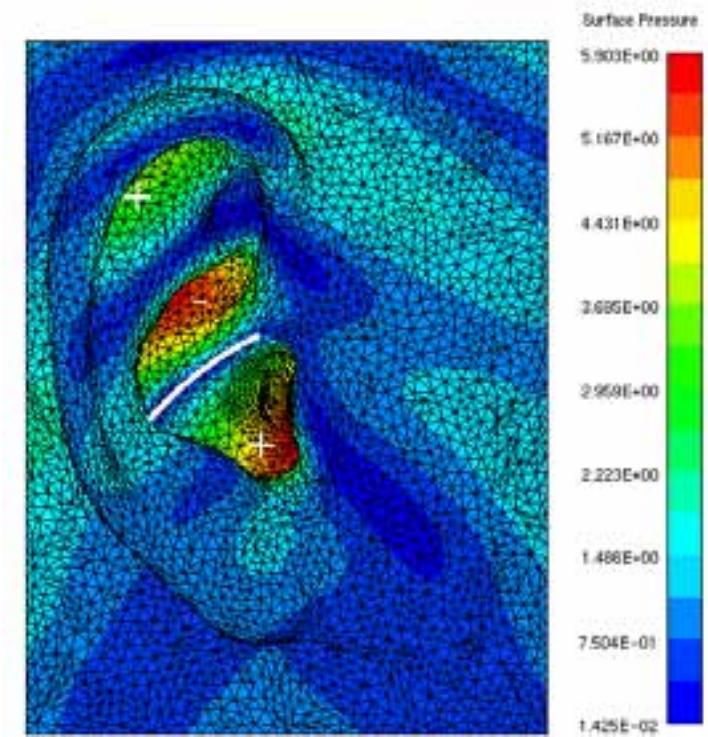
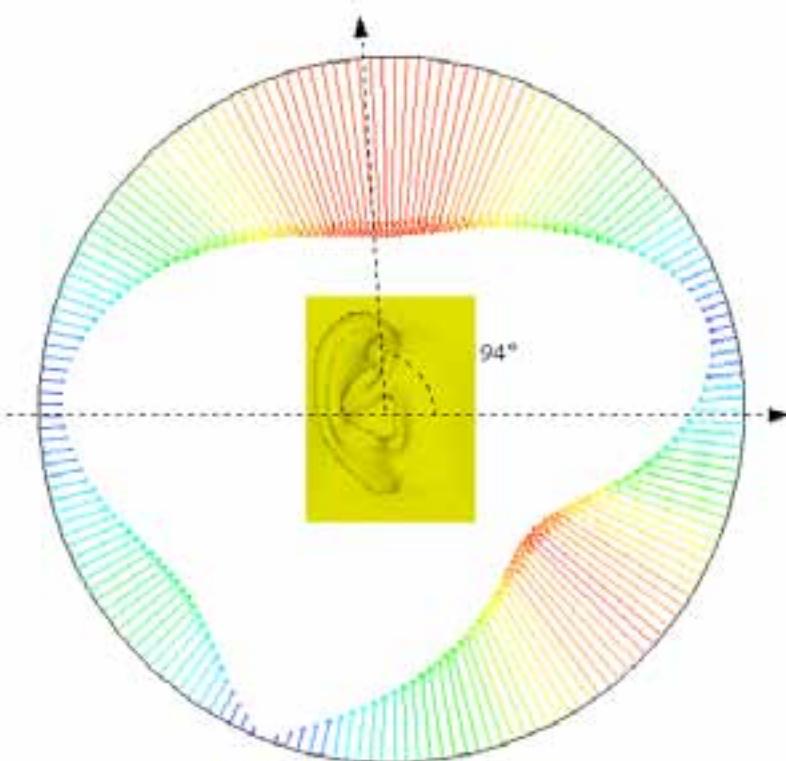
BEM SIMULATION OF THE MODE SHAPES OF THE DB65 PINNA – THE SECOND MODE

7.2 kHz



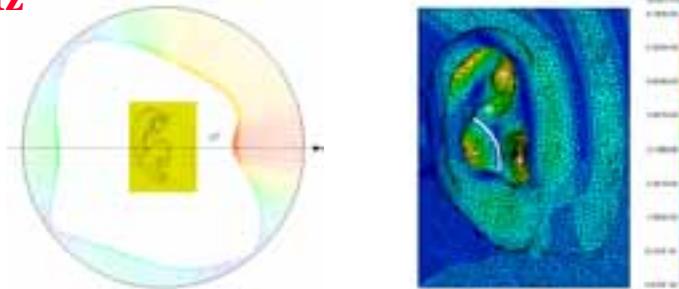
BEM SIMULATION OF THE MODE SHAPES OF THE DB65 PINNA – THE THIRD MODE

9.6 kHz

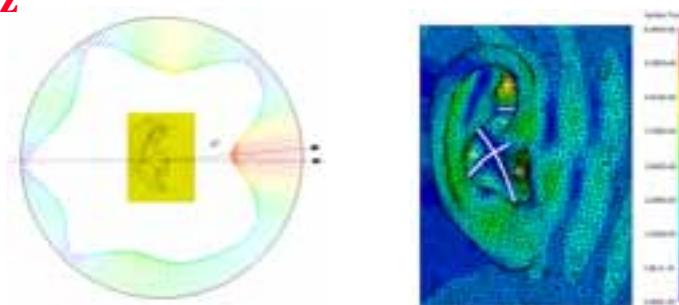


BEM SIMULATION OF THE MODE SHAPES OF THE DB65 PINNA – ‘HORIZONTAL’ MODES

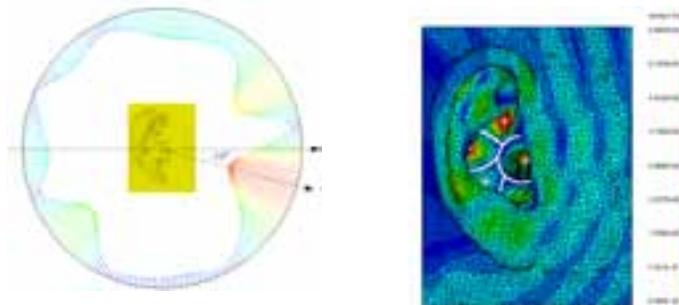
11.6 kHz



14.8 kHz



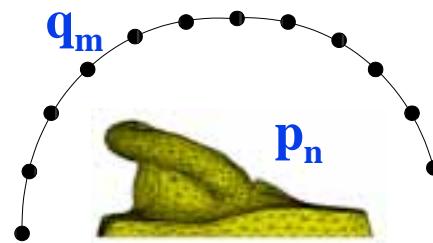
17.8 kHz



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SPATIAL PATTERNS IN ACOUSTIC SCATTERING



$$\begin{bmatrix} P_1 \\ P_2 \\ \vdots \\ \vdots \\ p_N \end{bmatrix} = \begin{bmatrix} G_{11} & G_{12} & \cdots & \cdots & G_{1M} \\ G_{21} & G_{22} & \cdots & \cdots & G_{2M} \\ \vdots & \vdots & \ddots & & \vdots \\ \vdots & \vdots & & \ddots & \vdots \\ G_{N1} & G_{N2} & & & G_{NM} \end{bmatrix} \begin{bmatrix} q_1 \\ q_2 \\ \vdots \\ \vdots \\ q_M \end{bmatrix}$$

or
 $\mathbf{p} = \mathbf{G}\mathbf{q}$

SINGULAR VALUE
DECOMPOSITION

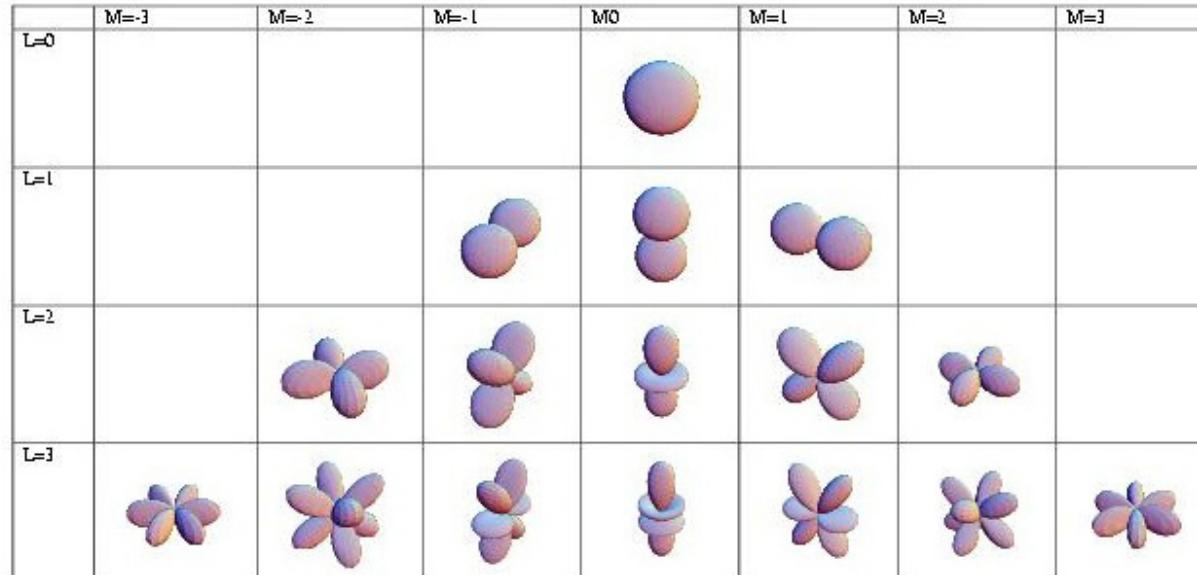
$$\longrightarrow \mathbf{G} = \mathbf{U}\Sigma\mathbf{V}^H$$

$$\mathbf{p} = \mathbf{U}\Sigma\mathbf{V}^H\mathbf{q} \quad (\mathbf{U}^H\mathbf{U} = \mathbf{U}\mathbf{U}^H = \mathbf{I})$$

$$\mathbf{U}^H\mathbf{p} = \Sigma\mathbf{V}^H\mathbf{q}$$

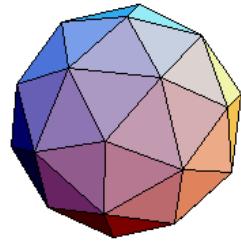
HRTF OF A RIGID SPHERE BASED ON SPHERICAL HARMONICS

$$Y_n^m(\theta, \phi) = (-1)^m \sqrt{\frac{2n+1}{4\pi} \frac{(n-m)!}{(n+m)!}} P_n^m(\cos\theta) e^{jm\phi}$$



$$p(\mathbf{r}) = j\rho_0 c_0 q(\hat{\mathbf{r}}) \sum_{n=0}^{\infty} \frac{h_n^{(2)}(kr)}{h_n^{(2)*}(ka)} \sum_{m=-n}^n Y_n^m(\theta, \phi) Y_n^{m*}(\hat{\theta}, \hat{\phi})$$

GREEN FUNCTION MATRIX RELATING POINTS ON A RIGID SPHERE AND SOURCES IN THE FAR FIELD (LARGE SPHERE)



$$\mathbf{G}(\mathbf{r} | \hat{\mathbf{r}}) = \begin{bmatrix} \sum_{n=0}^{\infty} f_n \sum_{m=-n}^n Y_n^m(\theta_1, \phi_1) Y_n^{m*}(\hat{\theta}_1, \hat{\phi}_1) & \dots & \sum_{n=0}^{\infty} f_n \sum_{m=-n}^n Y_n^m(\theta_1, \phi_1) Y_n^{m*}(\hat{\theta}_L, \hat{\phi}_L) \\ \sum_{n=0}^{\infty} f_n \sum_{m=-n}^n Y_n^m(\theta_2, \phi_2) Y_n^{m*}(\hat{\theta}_1, \hat{\phi}_1) & \dots & \sum_{n=0}^{\infty} f_n \sum_{m=-n}^n Y_n^m(\theta_2, \phi_2) Y_n^{m*}(\hat{\theta}_L, \hat{\phi}_L) \\ \sum_{n=0}^{\infty} f_n \sum_{m=-n}^n Y_n^m(\theta_K, \phi_K) Y_n^{m*}(\hat{\theta}_1, \hat{\phi}_1) & \dots & \sum_{n=0}^{\infty} f_n \sum_{m=-n}^n Y_n^m(\theta_K, \phi_K) Y_n^{m*}(\hat{\theta}_L, \hat{\phi}_L) \end{bmatrix}$$

$$\mathbf{G}_N(\mathbf{r} | \hat{\mathbf{r}}) = \begin{bmatrix} Y_0(\theta_1, \phi_1) & L & Y_n^m(\theta_1, \phi_1) & L & Y_N^N(\theta_1, \phi_1) \\ Y_0(\theta_2, \phi_2) & L & Y_n^m(\theta_2, \phi_2) & L & Y_N^N(\theta_2, \phi_2) \\ M & & & & \\ Y_0(\theta_K, \phi_K) & L & Y_n^m(\theta_K, \phi_K) & L & Y_N^N(\theta_K, \phi_K) \end{bmatrix} \begin{bmatrix} f_0 & & & & \\ & f_1 & & & \\ & & O & & \\ & & & f_N & \end{bmatrix} \begin{bmatrix} Y_0^*(\hat{\theta}_1, \hat{\phi}_1) & Y_0^*(\hat{\theta}_2, \hat{\phi}_2) & L & Y_0^*(\hat{\theta}_L, \hat{\phi}_L) \\ M & & & \\ Y_n^{m*}(\hat{\theta}_1, \hat{\phi}_1) & Y_n^{m*}(\hat{\theta}_2, \hat{\phi}_2) & L & Y_n^{m*}(\hat{\theta}_L, \hat{\phi}_L) \\ M & & & \\ Y_N^{N*}(\hat{\theta}_1, \hat{\phi}_1) & Y_N^{N*}(\hat{\theta}_2, \hat{\phi}_2) & L & Y_N^{N*}(\hat{\theta}_L, \hat{\phi}_L) \end{bmatrix}$$

$$\mathbf{G}_N(\mathbf{r} | \hat{\mathbf{r}}) = \mathbf{Y}(\mathbf{r}_k) \mathbf{F} \mathbf{Y}^H(\hat{\mathbf{r}}_l)$$

LINEAR TRANSFORMATION WITH UNITARY MATRICES

$$\mathbf{G}_N(\mathbf{r} | \hat{\mathbf{r}}) = \mathbf{Y}(\mathbf{r}_k) \mathbf{F} \mathbf{Y}^H(\hat{\mathbf{r}}_l)$$

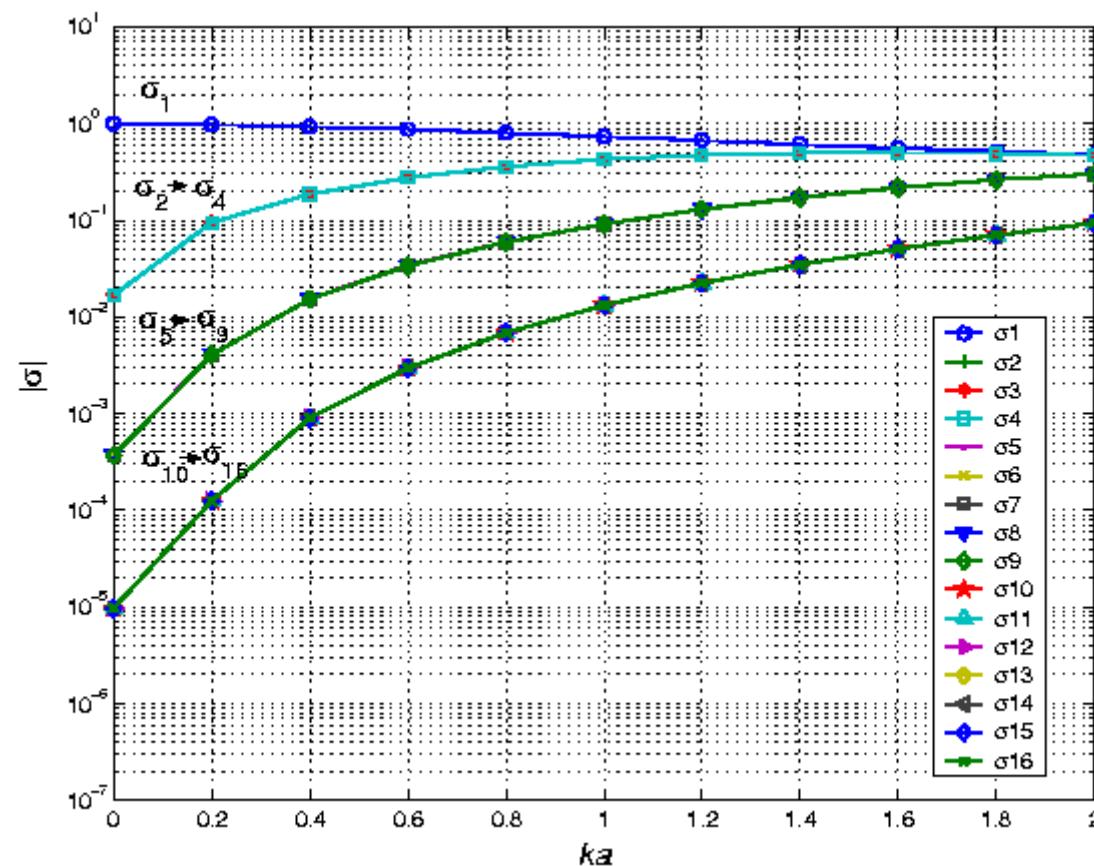
$$\mathbf{U}_N = \mathbf{Y}(\mathbf{r}_k) \mathbf{T}(\mathbf{r}_k)$$

$$\mathbf{V}_N = \mathbf{Y}(\hat{\mathbf{r}}_l) \mathbf{T}(\hat{\mathbf{r}}_l)$$

$$\mathbf{G}_N(\mathbf{r} | \hat{\mathbf{r}}) = \mathbf{Y}(\mathbf{r}_k) \mathbf{T}(\mathbf{r}_k) \underbrace{\sum_N \mathbf{T}^H(\hat{\mathbf{r}}_l) \mathbf{Y}^H(\hat{\mathbf{r}}_l)}_{\text{SVD}}$$

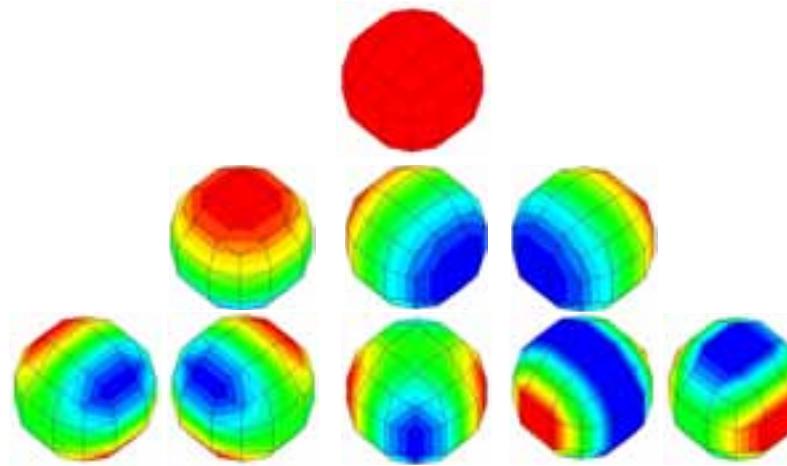
SVD: $\mathbf{G}(\mathbf{r} | \hat{\mathbf{r}}) = \mathbf{U} \mathbf{S} \mathbf{V}^H$

THE SINGULAR VALUES OF A 32x32 GREEN FUNCTION MATRIX WITH UNIFORMLY SAMPLED SPHERES

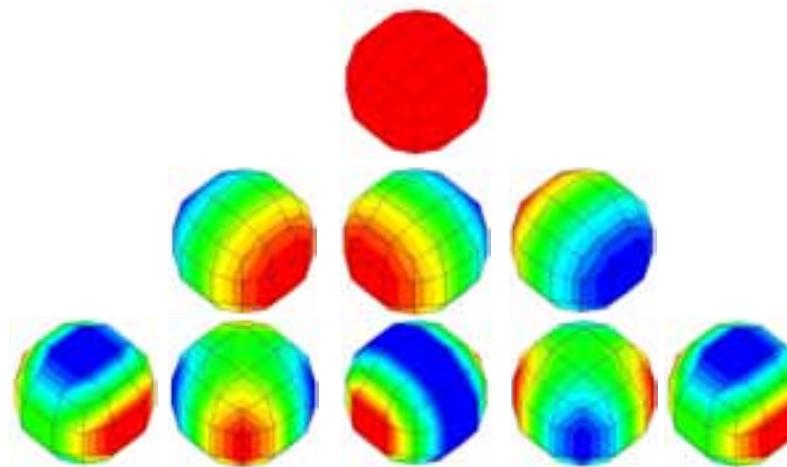


REAL PARTS OF SPHERICAL HARMONICS AND THE LEFT SINGULAR VECTORS OF THE GREEN FUNCTION MATRIX

$\text{Re}\{\mathbf{Y}(\mathbf{r}_k)\}$

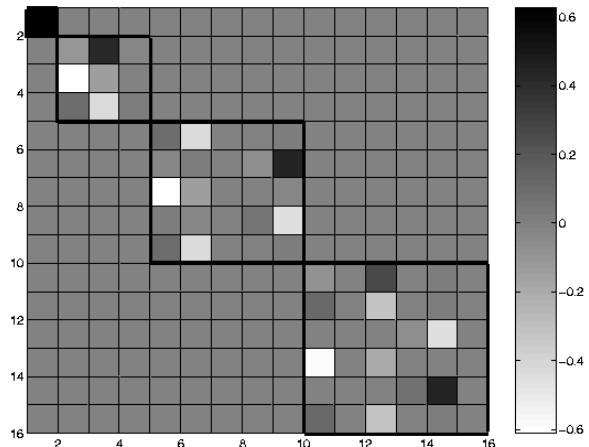


$\text{Re}\{\mathbf{U}(\mathbf{r}_k)\}$

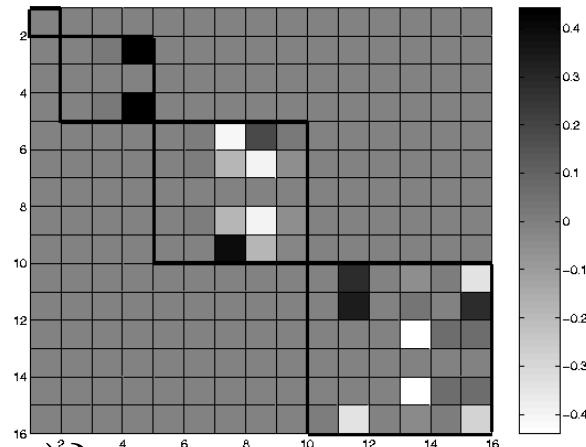


CALCULATION OF THE UNITARY TRANSFORMATION MATRICES

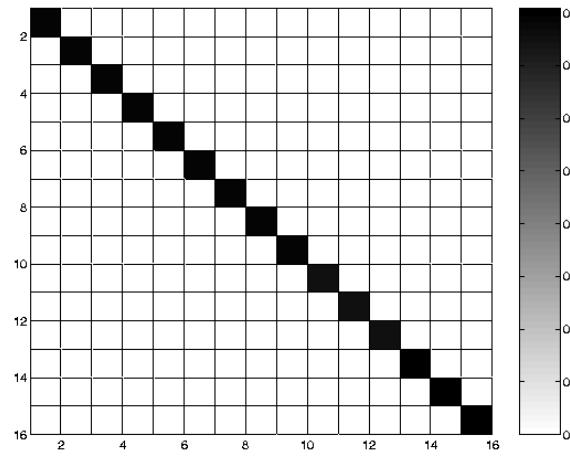
$$\text{Re}\{\mathbf{T}(\mathbf{r}_k)\}$$



$$\text{Im}\{\mathbf{T}(\mathbf{r}_k)\}$$



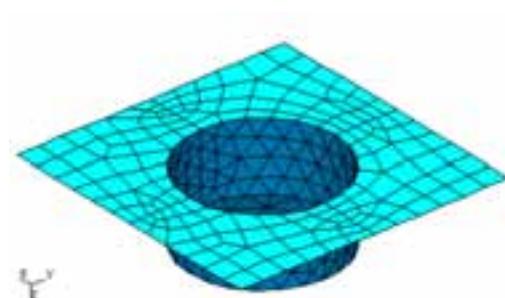
$$\text{Re}\{\mathbf{T}(\mathbf{r}_k)^H \mathbf{T}(\mathbf{r}_k)\}$$



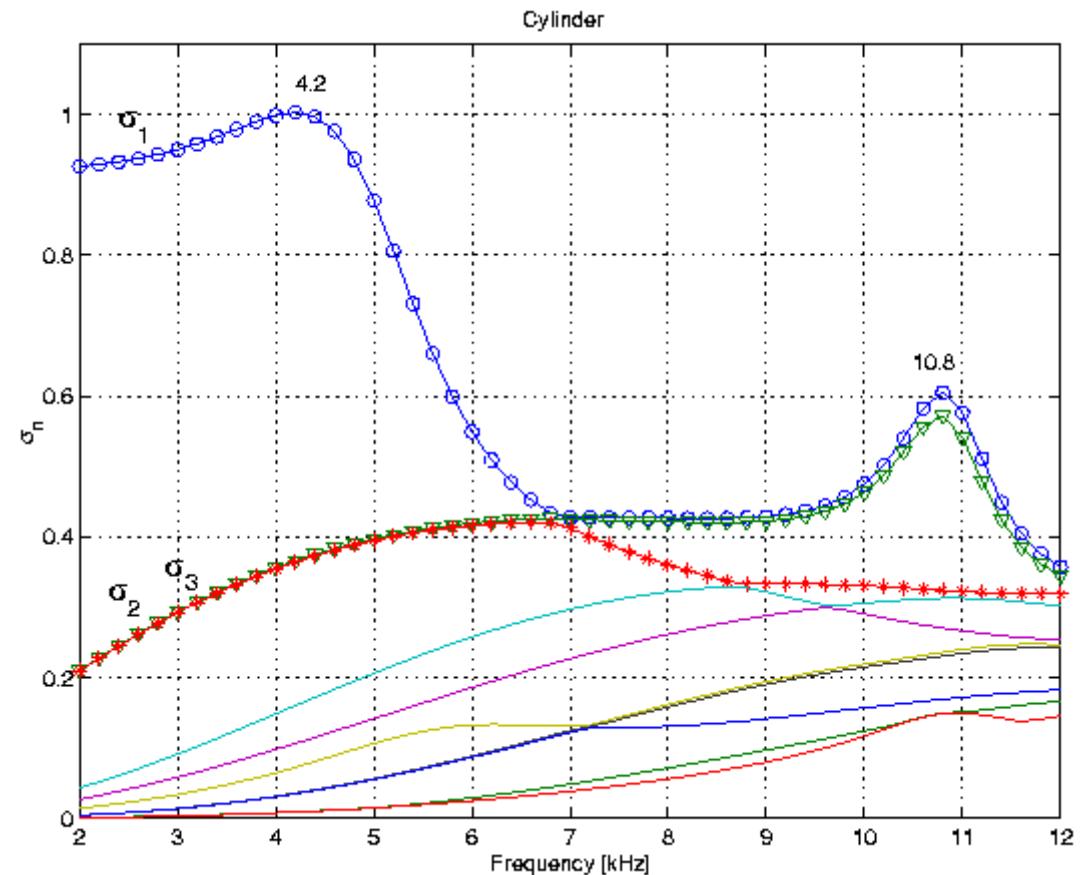
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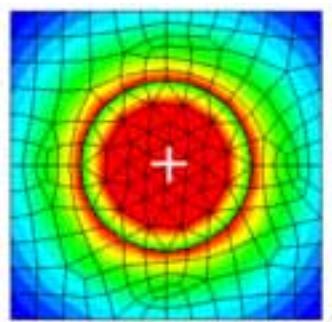
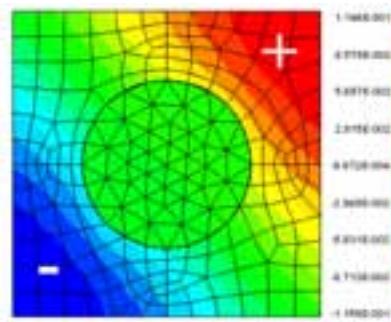
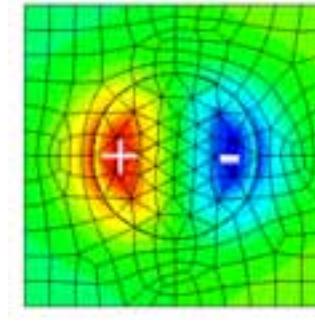
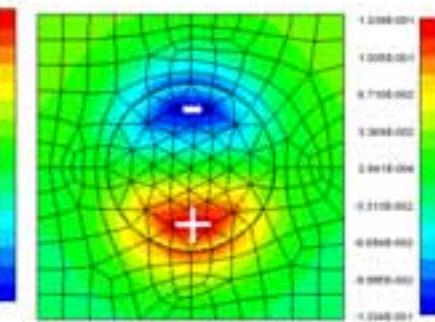
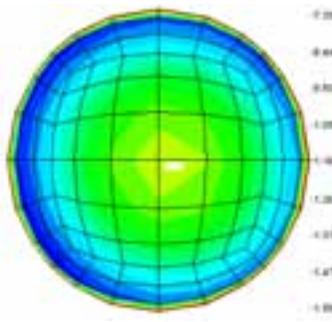
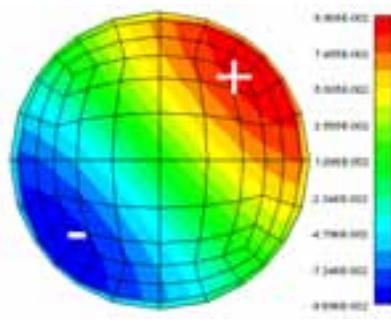
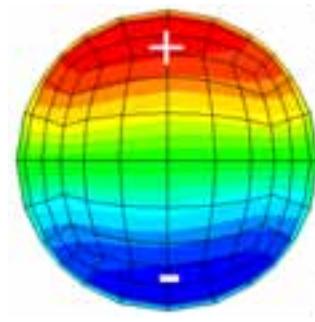
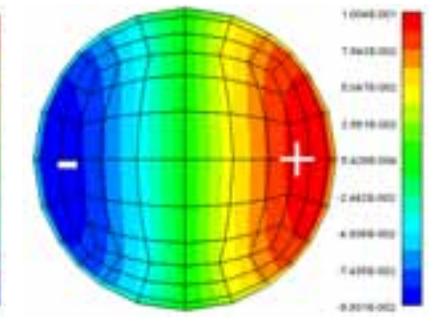
THE SINGULAR VALUES OF THE GREEN FUNCTION MATRIX RELATING A BAFFLED CYLINDER AND THE HEMISPHERE



356 'field' points
121 'source' points

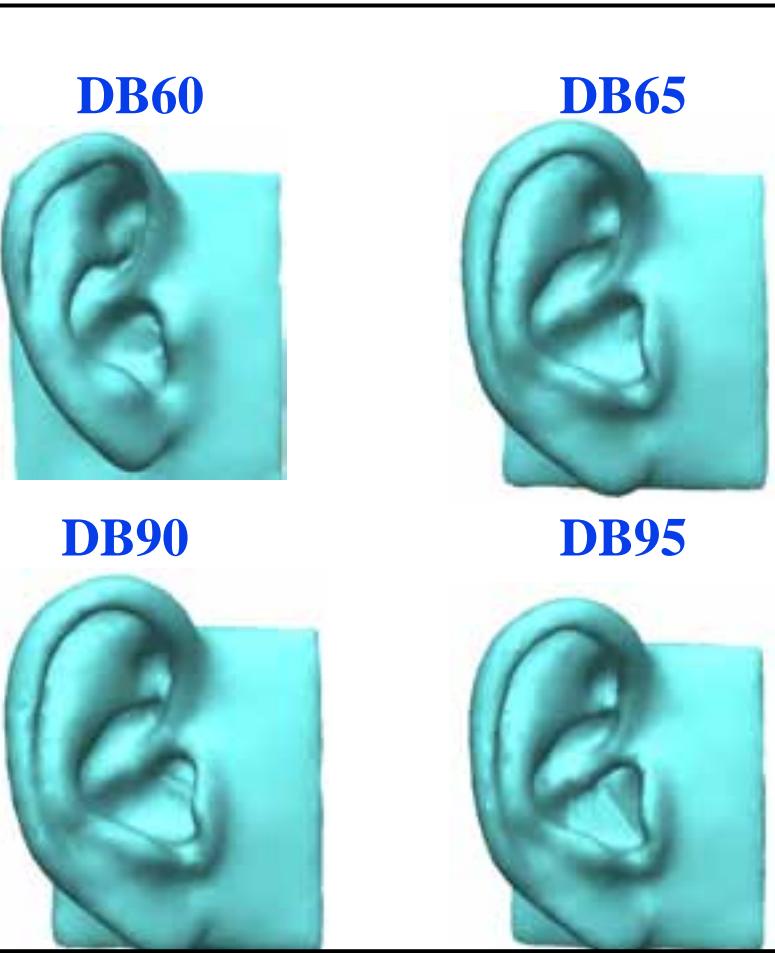


BAFFLED CYLINDER AND THE HEMISPHERE - COLOUR MAPS OF THE SINGULAR VECTORS

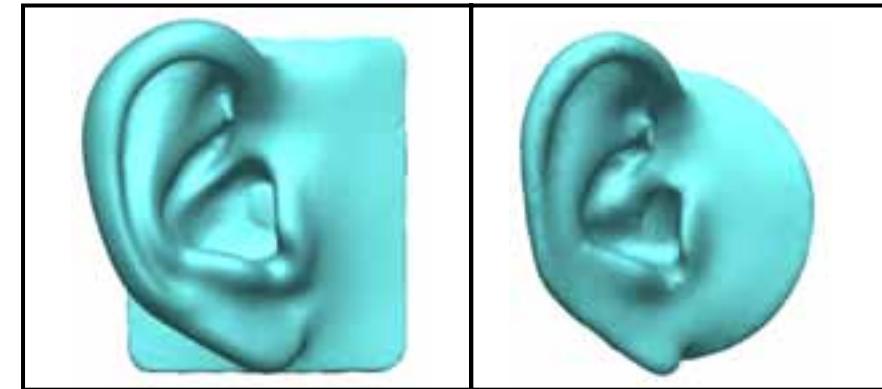
Re {v} σ_1 - 4.2 kHzRe {v} σ_2 - 4.2 kHzRe {v} σ_1 - 10.8 kHzRe {v} σ_2 - 10.8 kHzRe {u} σ_1 - 4.2 kHzRe {u} σ_2 - 4.2 kHzRe {u} σ_1 - 10.8 kHzRe {u} σ_2 - 10.8 kHz

MODELLLED PINNAE

KEMAR



B&K



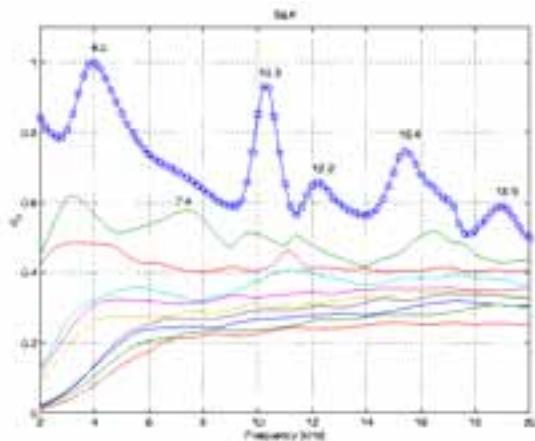
CORTEX



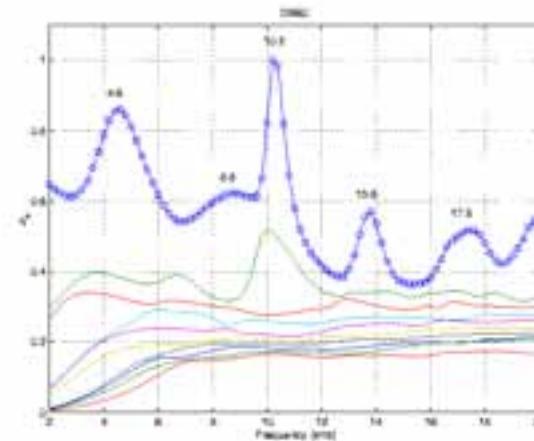
SINGULAR VALUES OF ACCURATE PINNAE

B&K

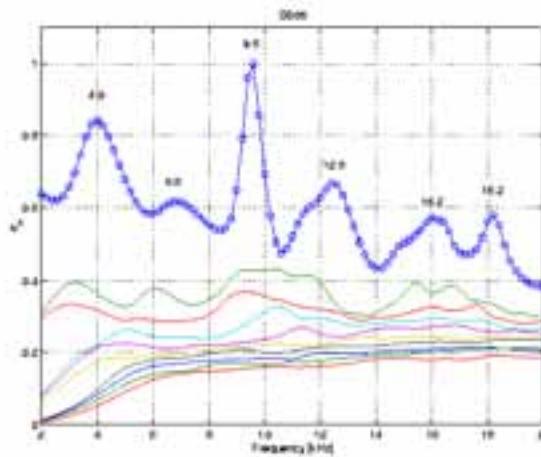
(3906 × 209)

**DB60**

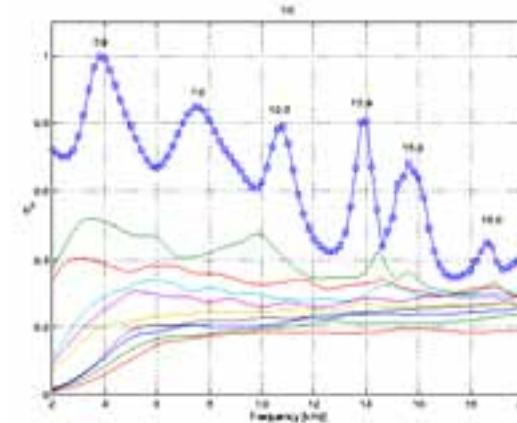
(2825 × 209)

**DB65**

(3389 × 209)

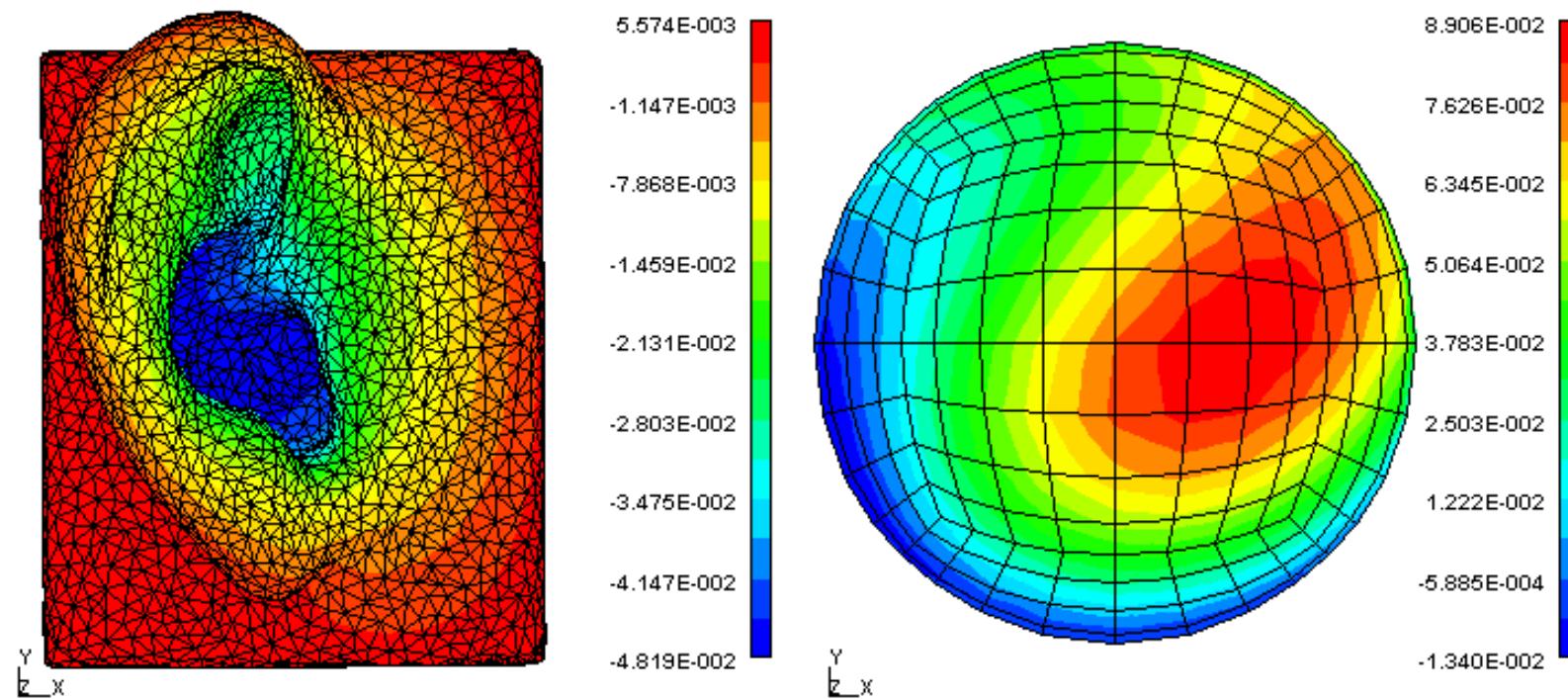
**YK**

(3392 × 209)



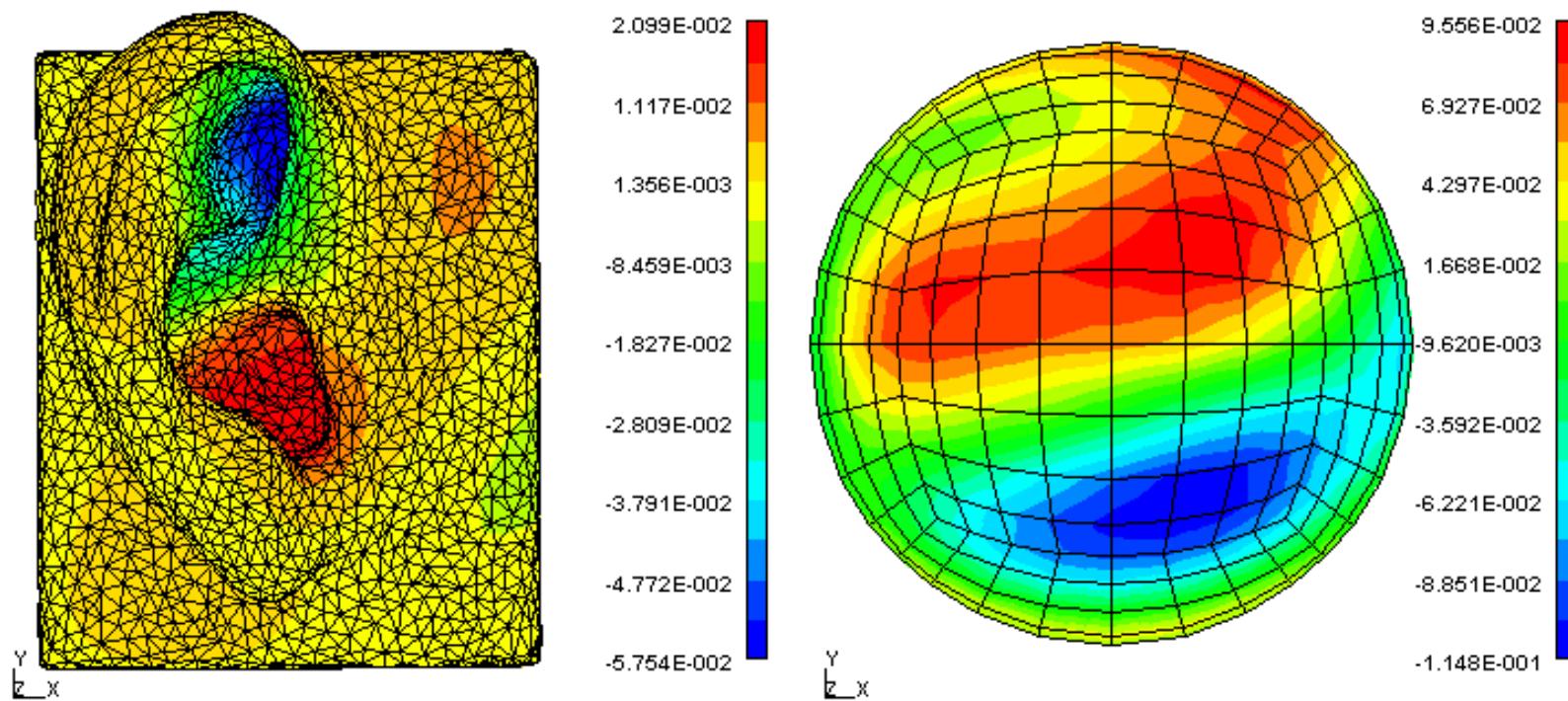
REAL PARTS OF THE SINGULAR VECTORS OF DB60

4.8 kHz



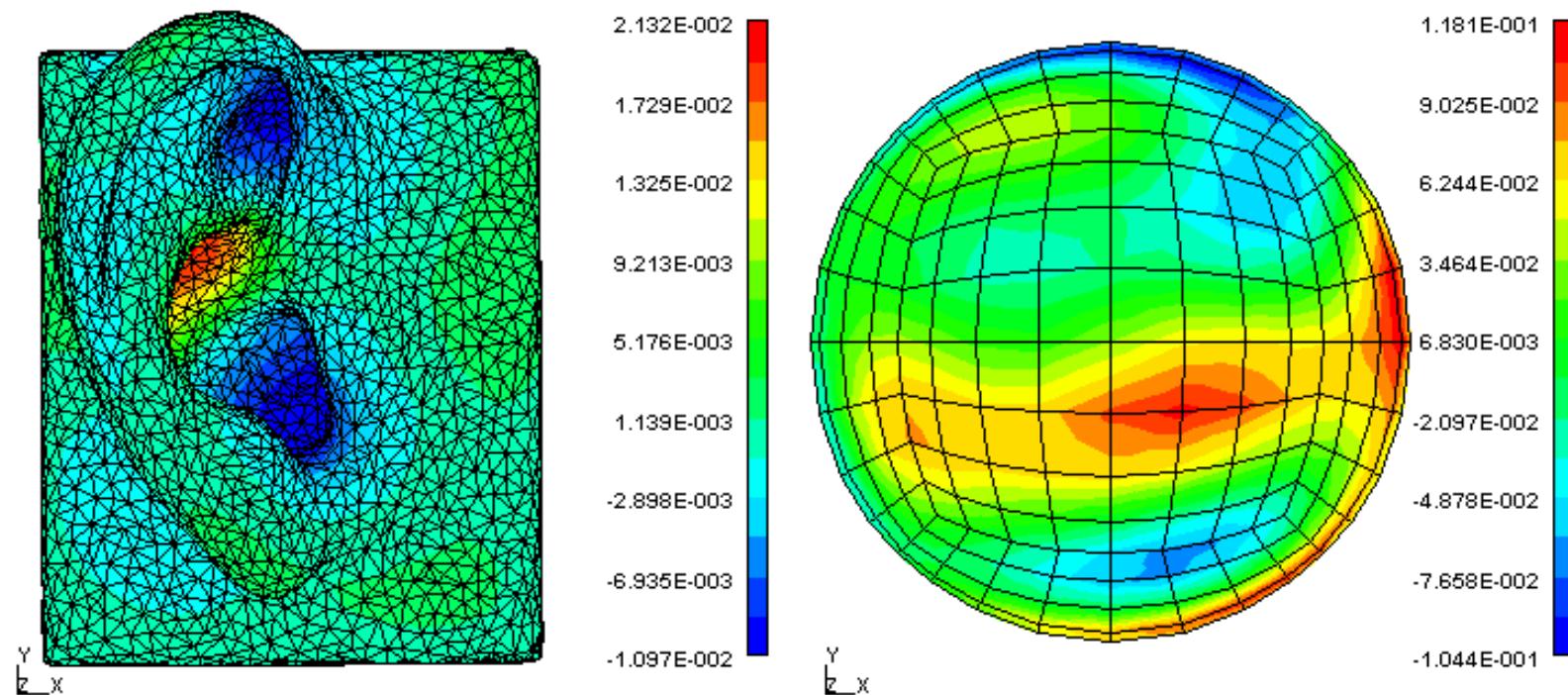
REAL PARTS OF THE SINGULAR VECTORS OF DB60

8.8 kHz



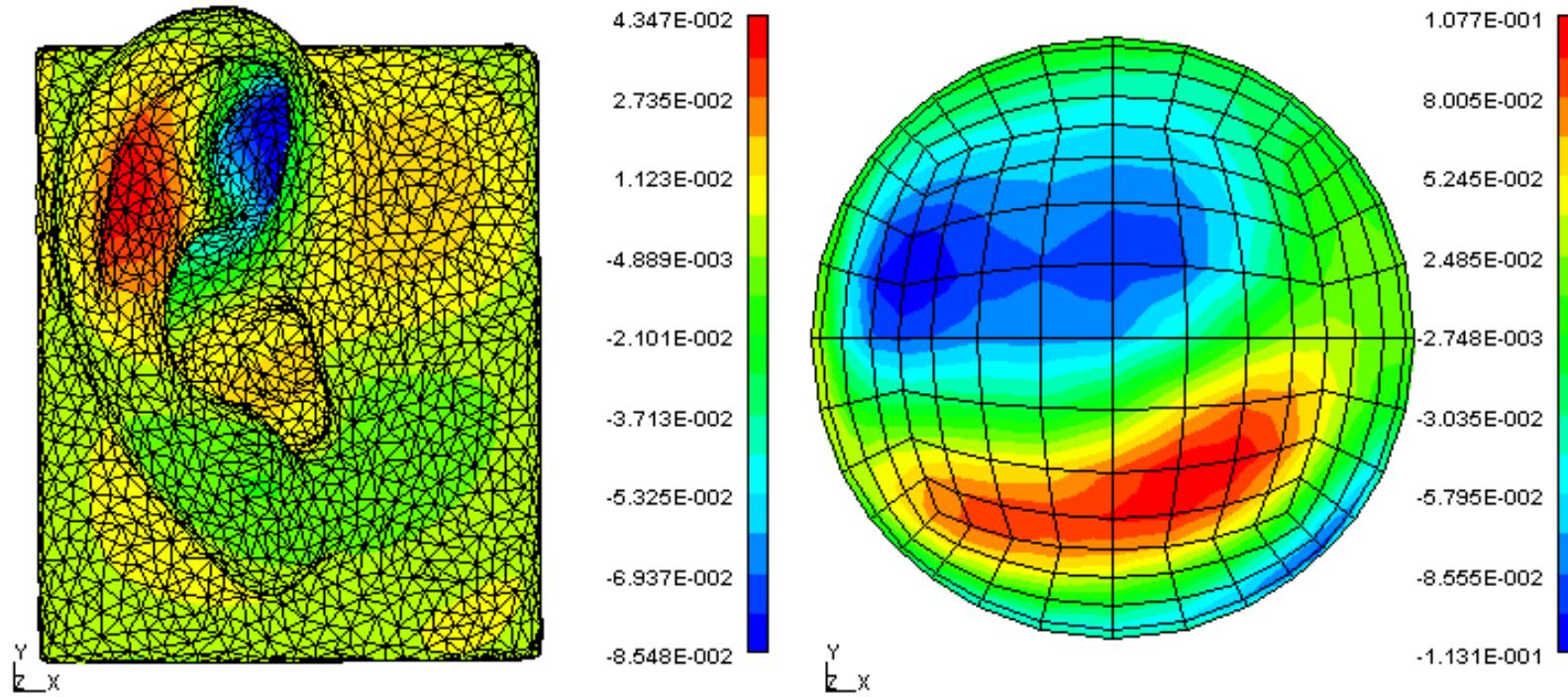
REAL PARTS OF THE SINGULAR VECTORS OF DB60

10.3 kHz / σ_1



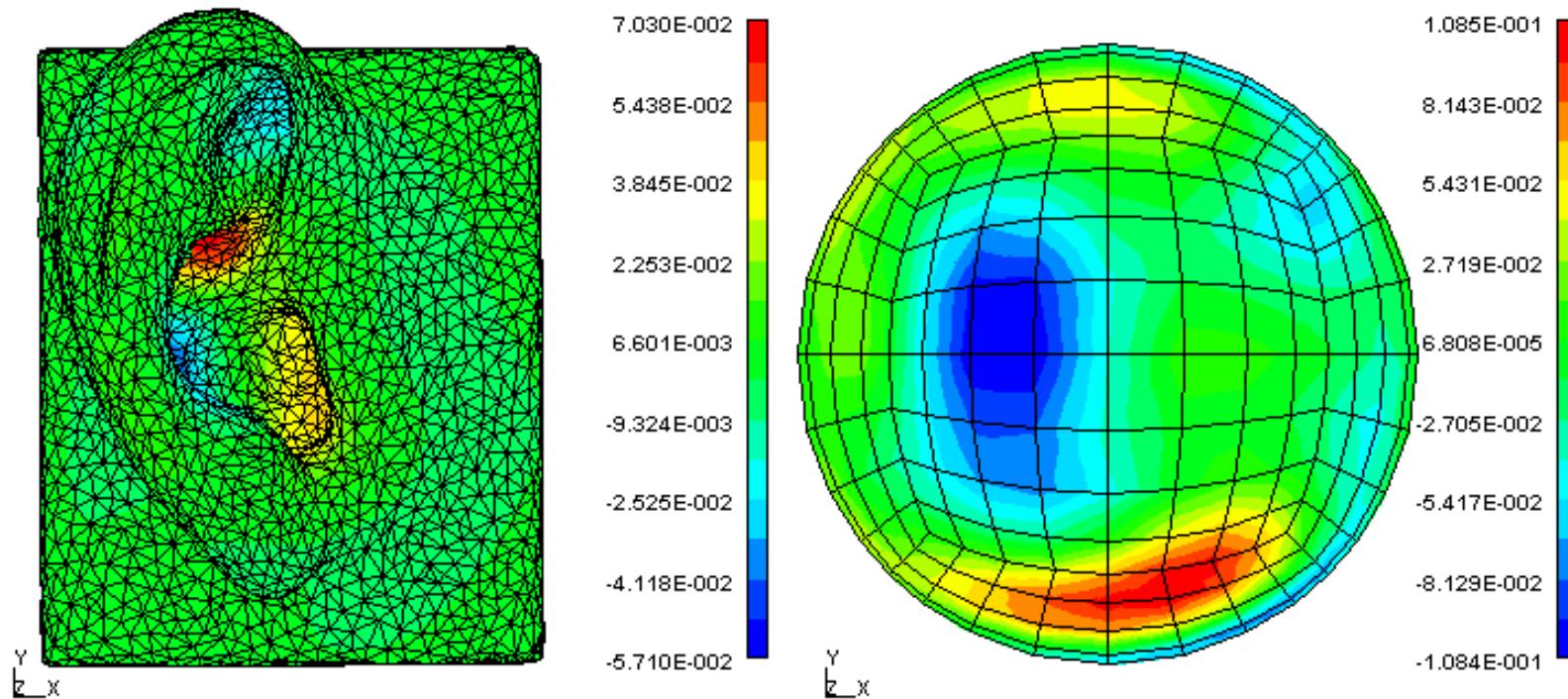
REAL PARTS OF THE SINGULAR VECTORS OF DB60

10.3 kHz / σ_2



REAL PARTS OF THE SINGULAR VECTORS OF DB60

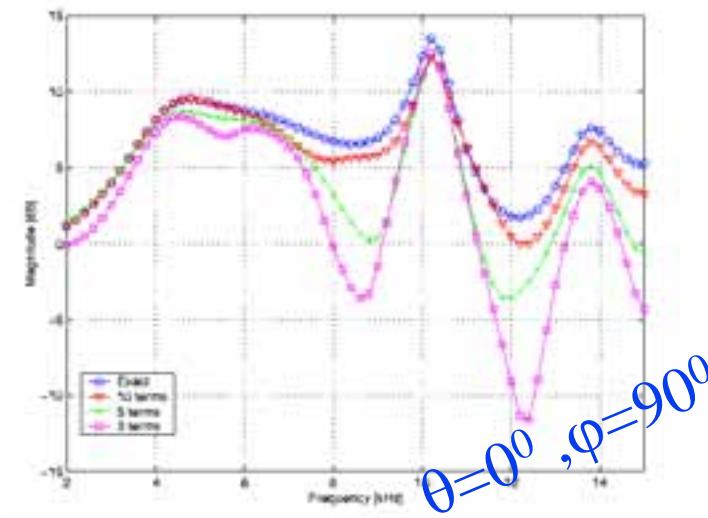
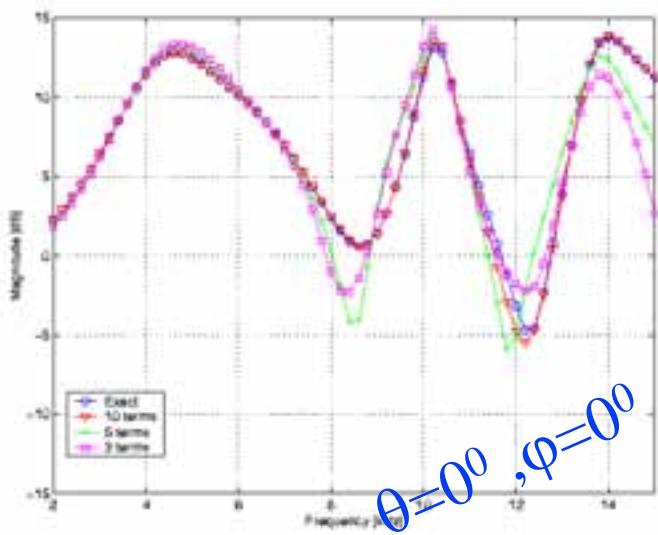
13.8 kHz



FREQUENCY RESPONSE DECOMPOSITION OF DB60 WITH TRUNCATED MATRICES

$$\begin{bmatrix} p_1 \\ p_2 \\ M \\ p_n \\ M \\ p_N \end{bmatrix} = \begin{bmatrix} u_{11} & u_{21} & L & u_{n1} & L & u_{N1} \\ u_{12} & u_{22} & L & u_{n2} & L & u_{N2} \\ M & M & O & M & M & M \\ u_{1n} & u_{2n} & L & u_{mn} & L & u_{Nn} \\ M & M & M & M & O & M \\ u_{1N} & u_{2N} & L & u_{nN} & L & u_{NN} \end{bmatrix} \begin{bmatrix} \sigma_1 \\ \sigma_2 \\ O \\ \sigma_n \\ O \\ \sigma_N \end{bmatrix} \begin{bmatrix} v_{11}^* & v_{12}^* & L & v_{1n}^* & L & v_{1N}^* \\ v_{21}^* & v_{22}^* & L & v_{2n}^* & L & v_{2N}^* \\ M & M & O & M & M & M \\ v_{m1}^* & v_{m2}^* & L & v_{mn}^* & L & v_{mN}^* \\ M & M & M & M & O & M \\ v_{M1}^* & v_{M2}^* & L & v_{MN}^* & L & v_{MN}^* \end{bmatrix} \begin{bmatrix} q_1 \\ q_2 \\ M \\ q_m \\ M \\ q_M \end{bmatrix}$$

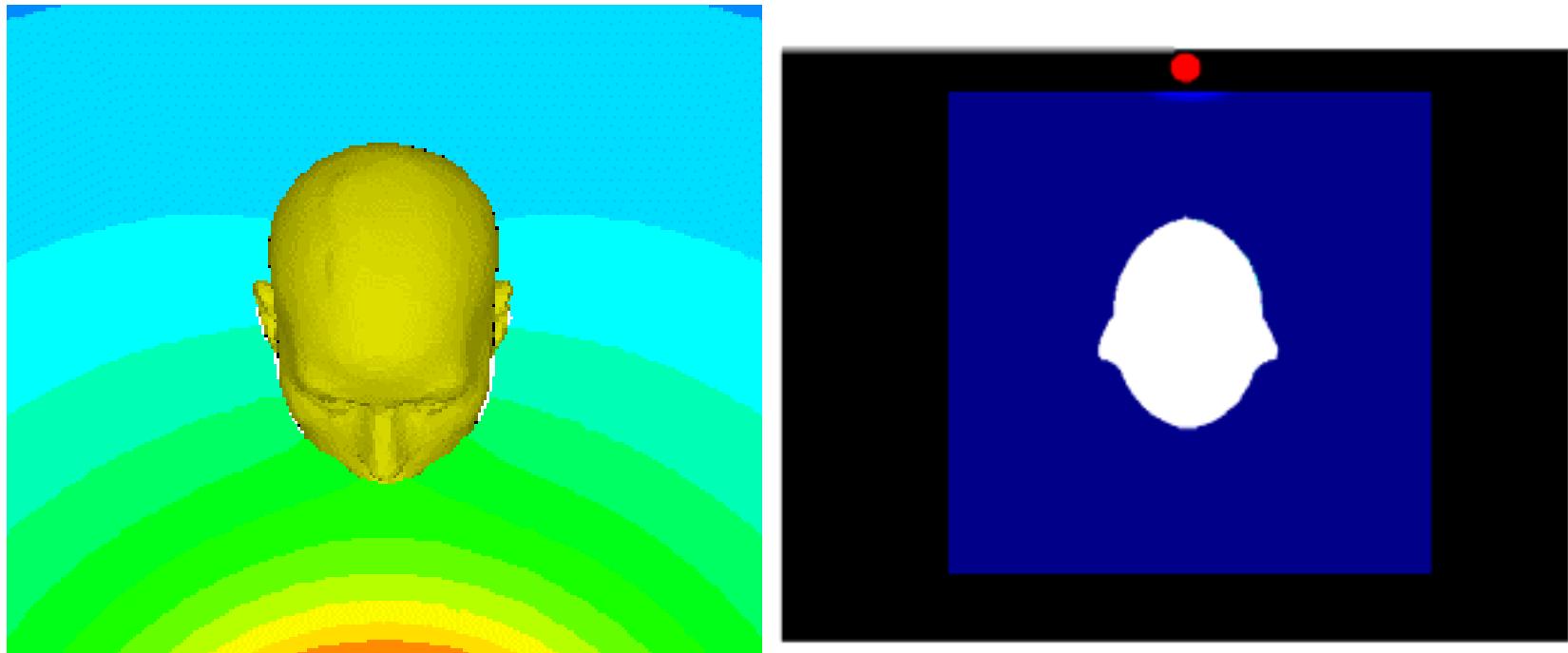
$$p_n = \sum_{n=1}^N \sigma_n u_{nn} v_{nm}^* q_m$$



Where are we?

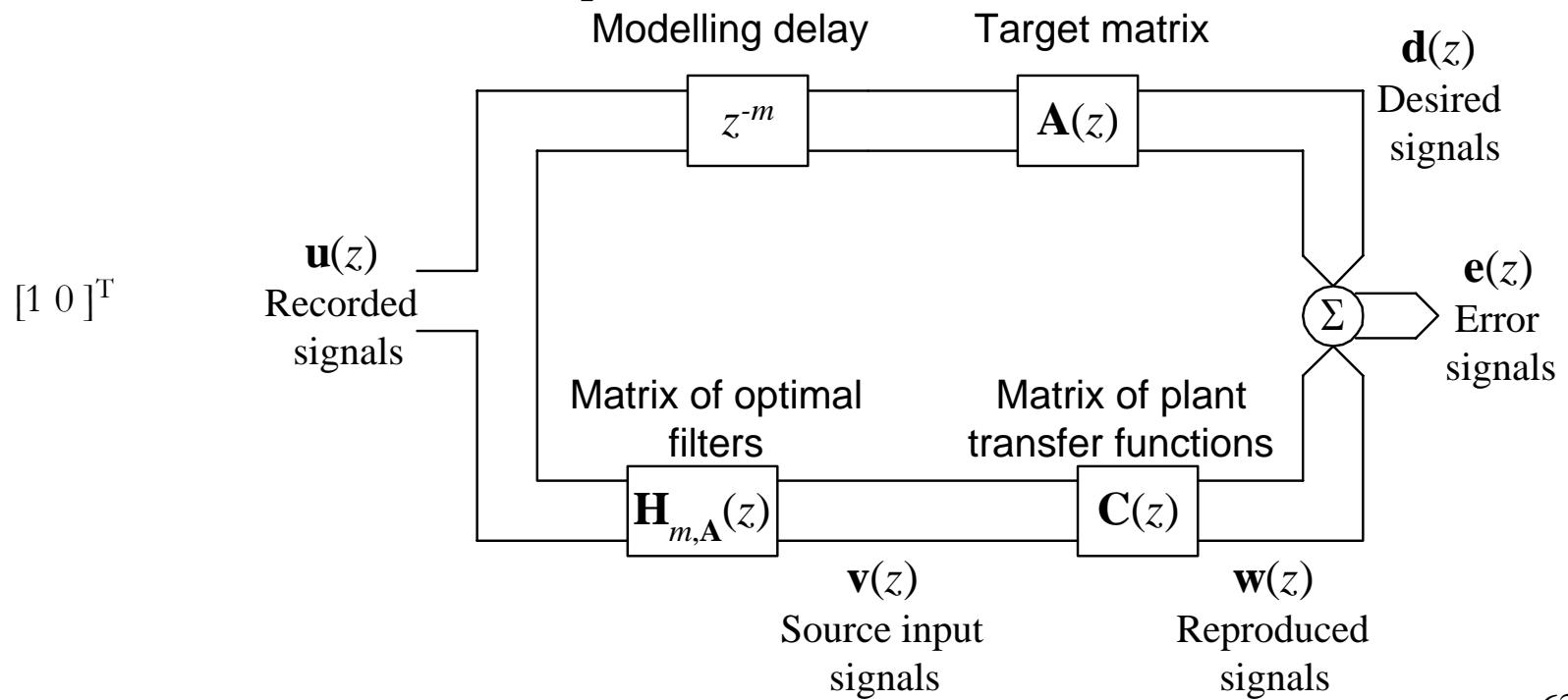
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SCATTERED SOUND FIELD AROUND KEMAR DUE TO A MONOPOLE - FREQUENCY AND TIME DOMAINS

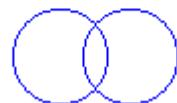
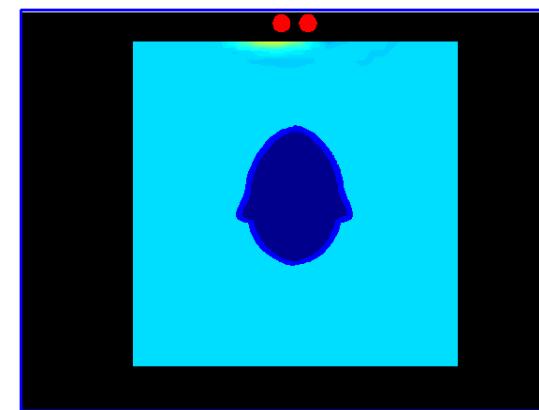
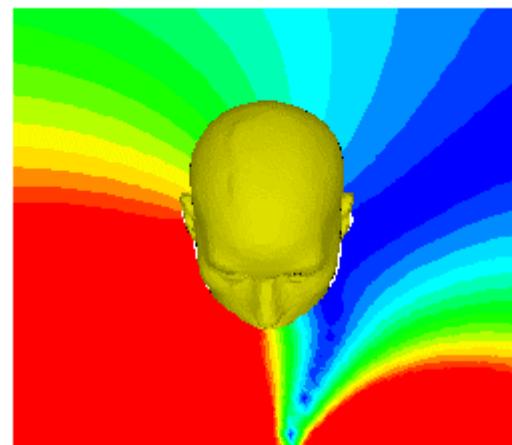
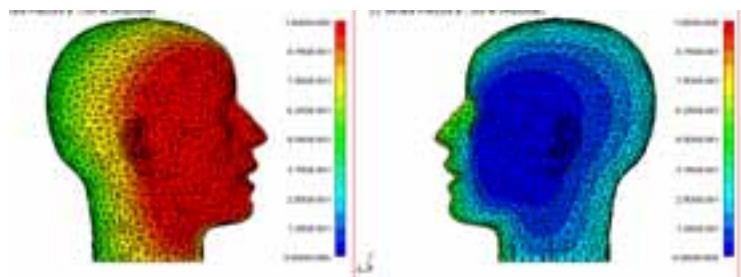


STEREO-DIPOLE VIRTUAL ACOUSTIC IMAGING SYSTEM

- Frequency domain - DC (1 Hz) to 6400 Hz, steps of 200 Hz
- Time domain - Digital Hanning pulse, impulse response of each field point
- Cross-talk cancellation - inverse problem



STEREO-DIPOLE FREQUENCY AND TIME DOMAIN ANIMATIONS



CONCLUSIONS

- Numerical modelling of HRTFs is NOT a trivial task.
- HRTFs can be modelled accurately to between 10-15 kHz, and the response of baffled pinnae can be modelled accurately up to 20 kHz.
- The accuracy of the laser scanner appeared to be significant for the analysis at high frequency.
- The normal mode shapes, as found by Shaw, were validated and investigated with numerical techniques rather than measurements.
- A connection between orthogonal basis functions and the SVD has been shown.
- “Mode shapes” can be found for any defined Green function matrix.
- The spatial patterns (of the six investigated pinnae) have similar shapes although with differences in magnitude and a slight shift in resonance frequencies.

CONCLUSIONS (cont.)

- It is possible to decompose a reduced order frequency response with only a few terms in the series for baffled pinnae.
- It is possible to visualise the sound field in the frequency and time domains for different arrangements of virtual acoustic imaging systems.